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# **Minority Serving College and University Cost Efficiencies**

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Abstract: Problem statement: Higher education minority enrollment growth has far outstripped white non-minority growth in the United States. Minority serving colleges and universities have disproportionately attended to that growth and will continue to play a critical role in providing minority educational opportunities in a knowledge based and globally diverse economy. However, they will face new and challenging budgetary and managerial reforms induced by the global financial crisis. As a result, they will be pressured to operate in the future with greater cost efficiency. Approach: Panel data pertaining to minority serving colleges and universities was used along with stochastic frontier analysis to provide cost inefficiency estimates over a four year academic period. Specification of an inefficiency component contained time varying institutional characteristics and influences, including a public Vs. private ownership control. Results: Minority College and university mean inefficiency was estimated to be approximately 1.24, indicating a 24% operation above the frontier cost. The study found that institutions achieved inefficiency reductions or efficiency gains in 2008-09 compared to 2005-06. The findings suggested that private institutions operated at greater inefficiencies relative to their publicly owned counterparts. However, the private sector laid claim to the most efficient institution, but also the most inefficient one. While the public minority serving colleges showed inefficiency deterioration over time, the findings point to private institution efficiency gains. Conclusion/Recommendations: A literature survey indicated that the study could be the first attempt at providing empirical estimates and subsequent insights into the operating cost efficiencies or inefficiencies of minority serving colleges and universities. The cost inefficiency findings suggested that these institutions did compare favorably in their managerial skills. However, as additional academic years of observations become available, they should be employed to determine the sustainability of the efficiency levels and gains uncovered in the present study.

Key words: Cost inefficiency, minority serving colleges and universities, stochastic frontier, Integrated Postsecondary Education Data System (IPEDS)

### **INTRODUCTON**

The purpose of this study is to provide empirical estimates of the operating cost efficiencies of minority serving colleges and universities in the United States. These colleges and universities are officially defined as having a minority student population that exceeds 50% of the total enrollment. They play a key role in serving an ever increasing racially and ethnically diverse population and preparing minorities for success in a global, knowledge based economy. The efficiency with which they produce higher education is critical to the need for their continued success, especially in view of the fact that the global financial crisis has and will continue to bring new budgeting models and management reforms to all of higher education. Thus, the operating cost efficiency of these minority colleges and universities should be of both public and managerial interest.

Li and Carroll (2007) puts the importance of minority enrollments in proper perspective. It reports that over the two decades 1994-2004, U.S. minority postsecondary enrollments increased 146% while white enrollments increased 15%. Black, Hispanic, Asian and American Indian enrollments increased from 18-32% of the total U.S. student enrollment. In addition, it is reported that minority serving colleges and universities played a disproportionately greater responsibility in that enrollment growth. Specifically, minority serving institutions enrolled 38% of all minority students in 1984. In 2004, that percent increased to 58%. Based on U.S. population projections, yet greater enrollment pressure may be placed upon these institutions. It is estimated that, between 2005-2020, the U.S. Hispanic

population will increase 77%, Black population by 32 and Asian by 69% (Kelly, 2005). A number of minority institutions are a century or more old, such as the Historically Black Colleges and Universities and Tribal Colleges and Universities in the U.S. Others are relatively new in minority status and are Hispanic or Asian serving institutions. And while minority enrollments have continued to increase at other socalled non-minority serving postsecondary institutions, it is obvious that the minority serving colleges and universities occupy a unique position in providing minority higher education opportunities.

To estimate the cost efficiency or inefficiency of minority serving colleges and universities the study employs stochastic frontier analysis using institutional panel data. The data take in a total of four academic years; 2005-09. Cost inefficiency is estimated as cost incurred above the minimum cost frontier. Thus, numerical measures of inefficiency can assume values of one or greater than one with the divergence from one being the extent of inefficiency. A Cobb-Douglas function is used to capture the underlying cost structure. The inefficiency component is specified as a being influenced by college and university characteristics, inefficiency potentially arising including from differences in ownership structure, viz., public compared to private non-profit colleges and universities. The time varying dynamics of institutional inefficiencies are explored over each of the four academic years.

#### MATERIALS AND METHODS

The development of stochastic frontier analysis used in this study is rooted in the seminal works of Aigner *et al.* (1977) and Meeusen and Broech (1977). Theoretical and methodological contributions building upon those works are plentiful and are well presented in Kumbhakar *et al.* (2003); Coelli (2005) and Fried *et al.* (2008). Although the general methodology is equally applicable to production and cost analysis, the interest in this study lies with the latter. In the panel data framework, the basic cost model for institution i in time period t can be expressed as Eq. 1:

$$C_{it} = X_{it}\beta + (u_{it} + v_{it}) \qquad i = 1, ..., N \qquad t = 1, ..., T$$
(1)

where, *C* is the total cost of production,  $X_{it}$  is an m×1 vector of outputs and input prices,  $\beta$  is a vector of unknown parameters and the error term contains two components. The v<sub>it</sub> portion of the error represents the usual random component that affects an institution's

technique. The Battesse and Corra (1977) reparameterization requires that  $\sigma^2 = \sigma_v^2 + \sigma_u^2$ . An estimate of  $\gamma = \sigma_u^2 / \sigma^2$  is produced and must, thereby, lie in the interval of zero to one. It can be employed to test if the frontier is stochastic. For  $\gamma = 0$  the inefficiency effects in Eq. 1 are irrelevant and other econometric techniques would be preferred for estimation purposes. For  $\gamma = 1$ , the random effects can be removed from Eq. 1 and all cost deviations would be due to institutional operating inefficiencies. Three studies involving efficiency estimates pertaining to higher education institutions employ some variation of the above formulation. Stevens (2005) estimates cost inefficiencies for a 1995-99 panel of 80 English and Welsh universities. The inefficiencies vary in the range of 1.007-2.011. Instead of cost

cost through exogenous shocks such as earthquakes,

tsunamis, or labor strikes. It can also be due to errors of

observation but is assumed to follow a normal

distribution with zero mean and variance  $\sigma_v^2$ . In

contrast, the nonnegative u<sub>it</sub> component measures cost

inefficiency due to environmental factors and factors

under the control of the institution. Inefficiency

influences can be embedded in certain characteristics of

the institution's inputs or can be due to managerial

decision-making within the institution. Under the

Battese and Coelli (1995) specification, these

inefficiency such that the uit are independently

distributed with a zero truncated normal distribution

with mean  $m_{it} = z_{it}\Delta$  and variance  $\sigma_u^2$ , where z is a

vector of inefficiency determinants and \* is a vector of

parameters to be estimated. The inefficiency of the ith

institution at time t can be determined by exp  $(u_{it})$ .

Being that the inefficiency component is non-negative

 $(u_{it}\geq 0)$ , the institutional inefficiency can assume

values greater than or equal to one, where any

deviation from the value of one indicates how far the

Maximum likelihood is the usual model estimation

institution operates above its cost frontier.

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environmental factors are assumed to

estimates cost inefficiencies for a 1995-99 panel of 80 English and Welsh universities. The inefficiencies vary in the range of 1.007-2.011. Instead of cost inefficiencies, McMillan and Chan (2006) estimate technical efficiencies for a 1992-93 cross section of 45 Canadian universities. Abbott and Doucouliagos (2009) also estimate technical efficiencies for their sample of 36 Australia (1995-2002) universities and 7 New Zealand (1997-2003) universities. The technical efficiencies of these studies appear to be in the range of 0.6-1.0 and indicate the extent to which institutions operate below their maximum potential output. While there are obvious relationships between cost inefficiencies and technical efficiencies, the results are masked by differences in the specific data and create an inability to reformulate the efficiency scores and place them on an equivalent scale to Stevens (2005) inefficiency scores. Two other higher education cost frontier studies are also of note but use different modeling assumptions. The Izadi et al. (2002) study uses a 1994-95 cross section of 99 British higher education institutions and Johnes and Johnes (2009) uses a 2000-03 panel data of 121 English institutions. Among all these studies, there exist substantial differences in the specification of the cost frontiers, the use of cross sectional time invariant vs. panel data inefficiency structures and the number of variables and their definitions used in the studies. As a result, comparative evaluations are beyond the ability and scope of the present inquiry.

In empirical studies, the vast majority of stochastic frontier analyses have used either the translog or Cobb-Douglas specification for the cost function. Preliminary investigations in the present study indicated that most of the translog coefficients failed to reach reasonable levels of statistical significance while the Cobb-Douglas revealed superior statistical performance. Therefore, the institution's cost (C) is modeled with a multi-product Cobb-Douglas form as follows Eq. 2:

$$\ln C_{ii} = \beta_0 + \sum_j \beta_j \ln Y_{ii,j} + \sum_k \beta_k \ln p_{ii,k} + (v_{ii} + u_{ii})$$
<sup>(2)</sup>

where, outputs and input prices are represented by the  $Y_i$  and  $p_k$  for the N universities over T academic years. In Eq. 2, empirical measures for the outputs and input prices are, of course, dependent upon data availability. Past studies have included full-time equivalent undergraduate and graduate enrollments as educational output measures, research grant revenues to proxy overall institutional research output and, in some cases, a faculty wage or average faculty salary for an input price (Cohn et al., 1989; Koshal and Koshal, 1999; Sav, 2004; Lenton, 2008). For the present specification, the same measures are employed but faculty wages are included for faculty on nine month salary contracts and for faculty on twelve month faculty contracts. Some institutions employ faculty under both contractual arrangements while others use one or the other for accounting purposes. In addition, to account for capital input prices, included is the year-end value of the institution's buildings. Thus, the three output measures along with the three input prices for empirical implementation of (2) are:

UGRAD	=	Full	time	equivalent	undergraduate
		enrol	lments,		
					-

GRAD	=	Full	time	equivalent	graduate
		enroll	ments,		

- RESCH = Research grant revenues,
- FACW9 = Nine month contract faculty wage based on average salary,
- FACW12 = Nine month contract faculty wage based on average salary,
- CAP = Capital price based on year-end value of buildings and for estimation purposes, all are in natural logarithms.

To take full advantage of the panel data, it is assumed that the operating cost efficiency of colleges and universities depends upon specific time varying institutional characteristics. First and foremost, that includes the minority level of the institution as measured by the percent minority student enrollment. But operating cost efficiency is also assumed to be influenced by overall student characteristics, including their financial ability to continue with their higher education pursuits and the quality of their primary and secondary schooling. A proxy intended to capture both is the percent of students enrolled that are on low income federal grants. The institutions ability to retain students can also affect cost efficiency. For underprepared students, some institutions, perhaps more than others, offer developmental courses and others engage better than others in providing student advising and non-instructional student services. The student retention rate serves as the aggregate institutional measure to capture the inter-institutional variation in the success of such endeavors. Student retention can be viewed as the result of a combined effort of faculty and administration. In contrast, the institutional debt is included in the inefficiency component as a better measure of internal managerial or administrative decision-making and skill.

Following Battese and Coelli (1995), these college and university characteristics are included in the inefficiency determination as follows Eq. 3:

$$u_{it} = \delta_0 + \sum_r \delta_r z_{r,it} + w_{it}$$
(3)

Where:

 $w_{it}$  = The normal random component

 $u_{it}$  = The truncated distribution with the mean being conditional on (3) and variance  $\sigma_u^2$ 

Based on the above Eq. 3, the z's are as follows:

All institutions		Public institut		Private institutions		
Variable	Mean	SD	Mean	SD	Mean	SD
С	8.23E+07	8.23E+07	1.35E+08	9.74E+07	4.14E+07	1.01E+08
UGRAD	3770.000000	3770.000000	6813.000000	7328.000000	1404.000000	1242.000000
GRAD	410.000000	410.000000	753.000000	916.000000	144.000000	334.000000
RESCH	1.47E+07	1.47E+07	2.48E+07	1.97E+07	6.85E+06	9.93E+06
FACW9	52028.000000	52028.000000	62201.000000	10088.000000	44116.000000	17942.000000
FACW12	5.14E+04	5.14E+04	6.29E+04	3.32E+04	4.24E+04	2.86E+04
CAP	1.03E+08	1.03E+08	1.72E+08	1.27E+08	4.93E+07	8.84E+07
MINORITY	81.660000	81.660000	81.610000	13.240000	81.710000	16.840000
LOWINC	64.380000	64.380000	60.830000	12.710000	67.150000	18.850000
RETENT	62.140000	62.140000	65.450000	9.880000	59.560000	16.740000
DEBT	36.390000	36.390000	35.890000	29.010000	36.780000	18.390000
CONTROL	0.560000	0.560000	0.000000	0.000000	1.000000	0.000000
Observations	512.000000		224.000000		288.000000	

MINORITY	=	Percent	student	minority
		enrollme	nt	
LOWINC	=	Percent	students on	low income
		Governm	nent grants	
RETENT	=	Full time	student retent	tion measured
		as studen	ts returning fa	ll term
DEBT	=	Percent 1	iabilities to as	sets
CONTROL	=	1 institu	tional contro	ol is private
		non-prof	it, 0 otherwise	-

The control variable is intended to measure the inefficiency differential that may potentially exist in ownership structures defined by private non-profit colleges and universities relative to public institutions. Ownership control is included as an inefficiency determinant not as an effect on cost structure. Thus, it is assumed that public and private non-profit colleges and universities have access to the same production technology and the same labor and capital markets. A Chow test on the ordinary least squares estimates indicated that there was no statistically significant difference in the cost structures and, therefore, separate ownership estimates of 1 and 2 could not be justified. However, as indicated in the results follow, there is a significant ownership effect on inefficiency.

Data: The U.S. Department of Education maintains a list of postsecondary institutions enrolling significant populations of minority students. The list is used to assist in determining institutional eligibility for specific federal grants and programs. The list of minority institutions in based on the enrollment data collected by the National Center for Education Statistics and housed in Integrated Postsecondary Education Data System (IPEDS). Colleges and universities on the list have been determined to report more than 50% of total enrollment as belonging to a minority group as defined by American Indian, Alaska Native, Black and Hispanic. Enrollment is

defined at the postsecondary undergraduate level, although some of the same institutions engage in graduate education. Institutions with Asian-American student populations may be classified as minority institutions for certain federal programs but may not be on this list. Public and private non-profit colleges and universities are included on the list but the Department excludes for-profit institutions.

For panel data estimation, the most recent four academic years, 2005-09, of surveys are obtained from IPEDS. The minority institutions list was merged with the IPEDS surveys and institutions were omitted that failed to report necessary cost and enrollment data. The final useable sample included an unbalanced set of 128 colleges and universities for a total of 512 observations.

Table 1 presents the means and standard deviations of the cost and inefficiency variables. The summaries are presented for all institutions combined and separately for public and private colleges and universities. The total cost measure is the academic year total operating expenditures. Interestingly, on average, public and private sectors have nearly identical minority enrollments at approximately 82%. Public institutions, however, have substantially greater undergraduate enrollment, graduate enrollment and research outputs. In addition, publics have higher wage structures for both nine and twelve month contract faculty. Public institutions also have a slightly higher student retention rate but a lower percentage of students on low income grants. Both ownership structures carry approximately the same debt.

# **RESULTS AND DISCUSSION**

The frontier estimates are presented in Table 2. At the 1% level of statistical significance the likelihood ratio indicates that the frontier estimates are to be favored over an ordinary least squares

Table 2. Institution frontier estimates

technique. In addition, \* is statistically significant at well above the 1% level and, therefore, indicates that inefficiency is present in affecting the overall costs of minority colleges and universities. That is, the share of inefficiency in the combined error is approximately 87%.

Overall, the cost model performs well. All of the output coefficients as well as the nine month faculty wage and the capital price proxy are statistically significant at better than the 1% level of significance. In addition, they all carry the expected cost increasing effect. Although the twelve month faculty wage enters with the unexpected negative sign, it fails to reach any reasonable level of statistical significance. For the Cobb-Douglas specification, the coefficients are the cost elasticities. Thus, for a 1% increase in undergraduate enrollments, there occurs an estimated 0.444% increase in college and university costs. Among the three outputs, that is by far the largest cost elasticity. A 1% increase in graduate education or research produces a cost increase of only a 0.057 and 0.011%, respectively. As would be expected, capital improvements carry greater cost increases relative to increased faculty wages.

Equally encouraging are the results for the inefficiency specification. Positive coefficients indicate increases in inefficiency and, therefore, negative coefficients can be viewed as efficiency improvements. Thus, increases in minority enrollments lead to increased efficiency and suggest that these institutions are adept at minority education. However, has indicated, its effect is statistically insignificant, indicating that perhaps the marginal effect would be only slight given that minority student enrollments are already at high levels. Somewhat counter intuitive is the efficiency improvement effect associated with increased enrollment of low income grant recipient students. However, if such students are generally of like social and economic backgrounds, then it is possible that it is more efficient for the institution to produce education and student services for more homogenous student populations, i.e., more specialization in this sense may offer efficiency gains. Yet, the coefficient for the retention variable indicates that institutional attempts to increase student retention tends to create inefficiency, but not to a high degree of statistical significance.

Of all the inefficiency determinants, institutional debt is estimated to have the largest inefficiency impact. And while as currently employed it is not likely to be a complete measure of internal management decision-making skills, it does support the general view that debt management, at least beyond some point.

	Standard					
Variable	Coefficient	Error	t value			
Cost						
Constant, $\beta_0$	6.143	0.240	*25.62			
UGRAD	0.444	0.022	*20.59			
GRAD	0.057	0.005	*11.15			
RESCH	0.011	0.004	*2.42			
FACW9	0.014	0.006	*2.41			
FACW12	-0.001	0.003	-0.42			
CAP	0.417	0.020	*21.05			
Inefficiency						
Constant, $\delta_0$	-3.895	1.033	*-3.77			
MINORITY	-0.163	0.183	-0.89			
LOWINC	-0.222	0.088	*-2.53			
RETENT	0.078	0.067	1.17			
DEBT	1.031	0.054	*19.06			
CONTROL	0.767	0.121	*6.35			
$\sigma^2$	0.287	0.045	*6.30			
γ	0.872	0.026	*33.78			
ĹL	-8.929	-	-			
LL Ratio	*116.398	-	-			

Generates cost inefficiency impact. The ownership control variable is the final inefficiency determinant and its positive coefficient reveals greater operating cost inefficiencies among private non-profit relative to publicly owned minority colleges and universities. That differential ownership effect is explored in greater detail in what is to follow.

Table 3 provides the calculated cost inefficiency scores as aggregated over the four academic years and for each individual academic year. In addition, inefficiency scores are decomposed by ownership sector. For all minority institutions, the 2005-09 mean inefficiency score is 1.237 indicating that institutions operated at about 24% above their cost frontiers. However, it is noted that institutions managed substantial efficiency improvements over the four years as inefficiency scores fell from 1.283 in 2005-06-1.229 in 2008-09; but there were slight increases incurred from the low of 1.211 achieved in 2006-07. Overall, those efficiency gains came through reductions in the maximum inefficiency scores and little noticeable change in the minimum inefficiency scores. On that account, the inter-sector decomposition indicates that the private sector lays claim to both the minimum inefficient and the maximum inefficient institution. And on average, for the 2005-09 periods, privately owned minority colleges operated at a higher inefficiency relative to their public counterparts: but it was only 12% higher (1.298 Vs. 1.159). That is also true of the median public vs. private inefficiency, but the 2005-09 difference is only 6%. Comparing the 2005-06 academic year to the 2008-09 academic year, the public sector incurred an increased inefficiency while the private sector achieved an efficiency improvement.

	ficiency estimates by year and control All Minority Institutions				
Year	05-09	05-06	06-07	07-08	08-09
Mean	1.237	1.283	1.211	1.230	1.229
Median	1.149	1.144	1.142	1.151	1.156
S.D.	0.328	0.465	0.238	0.260	0.294
Skewness	5.399	4.607	4.793	4.500	5.532
Minimum	1.031	1.036	1.033	1.033	1.031
Maximum	4.196	4.196	2.845	3.032	3.360
Ν	512.000	128.000	128.000	128.000	128.000
Public mino	rity instituti	ions			
Mean	1.159	1.144	1.149	1.166	1.176
Median	1.118	1.104	1.113	1.127	1.138
S.D.	0.134	0.116	0.127	0.147	0.145
Skewness	3.116	2.905	3.314	3.317	2.926
Minimum	1.042	1.042	1.050	1.060	1.055
Maximum	1.844	1.618	1.764	1.844	1.757
Ν	224.000	55.000	56.000	56.000	57.000
Private min	ority institu	tions			
Mean	1.298	1.389	1.259	1.273	1.271
Median	1.184	1.200	1.184	1.184	1.167
S.D.	0.410	0.590	0.288	0.316	0.369
Skewness	4.416	3.513	4.229	3.967	4.718
Minimum	1.031	1.036	1.033	1.033	1.031
Maximum	4.196	4.196	2.845	3.032	3.360
Ν	288.000	73.000	72.000	72.000	71.000

Table 4: Inefficiency distributions by control

	All	Public	Private
Percentile	institutions	institutions	institutions
5th	1.066	1.063	1.070
10th	1.079	1.071	1.083
25th	1.103	1.092	1.124
50th	1.149	1.119	1.185
75th	1.252	1.167	1.306
90th	1.411	1.252	1.468
99th	3.032	1.757	3.360

Table 4 compares the percentile distributions of inefficiency scores. At the 25th and below percentiles, there is little difference in the public and private inefficiency densities. At the median, 50th percentile, the divergence in the public-private densities begins to widen. Beyond the 50th percentile, the private college and university distribution tails out to larger inefficiencies and exhibits the larger positive skewness relative to the public institutions.

# CONCLUSION

The main thrust of this study was to empirically investigate the cost efficiency of producing higher education among minority serving colleges and universities in the United States. That inquiry seemed to be of particular importance given the increases in minority enrollments in the U.S. and the apparent disproportionate share of those enrollments being attended to at minority serving colleges and universities. Given the critical role these institutions have played in minority higher education, projected minority population growth suggests that future educational demands could bring serious resource and financial pressures to bear upon management. That, along with changes in higher education finances driven by the global financial crisis, provided the impetus for the current study. Likewise, the inquiry should bring public and managerial interest along with it.

Minority college and university panel data was used in stochastic frontier analysis to provide empirical estimates of operating cost inefficiencies. The overall four year, 2005-09, mean inefficiency estimate was approximately 1.24 while the median was 1.15. Thus, minority serving institutions were estimated to operate on average at about 24% above their minimum frontier costs. Fifty percent of the institutions, however, were below 15%. The findings indicate that the aggregate of institutions managed to put into place a substantial efficiency gain (inefficient reduction) from the 2005-06 to the 2008-09 academic year. When results were decomposed by public Vs. private non-profit institutions, the findings showed that private minority colleges and universities operate more inefficiently than their public counterparts. The average private inefficiency score was approximately 1.30 while the public score came in at 1.16. However, in each academic year and overall, the private sector laid claim to the most efficient operating institution. At the same time, it offered the most inefficient institution. As a group, the public sector inefficiencies deteriorated from the 2005-06 to the 2008-09 academic years while private institutions developed efficiency improvements.

There are no comparable minority college and university cost efficiency estimates that can serve as benchmarks to the current study. Although not directly comparable, Stevens (2005) did employ a similar methodology and provided cost inefficiency estimates for English universities in the range of 1.007-2.011. With that, one would be inclined to conclude that the current group of U.S. minority colleges and universities compare very favorably in terms of cost efficiency. Future research agendas might take interest in exploring cost efficiencies in other minority serving institutions. In addition, as future academic years of observations become available for the current group of minority colleges and universities, it would be of interest to determine the managerial ability of these institutions to generate greater efficiency gains in the offering of minority higher education.

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