

Bioaccumulation of Cr(III) ions by Blue Green-alga *Spirulina* sp. Part II. Mathematical Modeling

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Abstract: In the present paper bioaccumulation of Cr(III) ions by blue-green algae *Spirulina* sp. is discussed. We found that the process consisted of two stages: passive in which Cr(III) ions are bound to the surface of cells, identical with biosorption and active, metabolism-dependent, in which Cr(III) ions are transported into the cellular interior. The passive stage occurs in both living and non-living cells and the active – only in living biomass. Two distinctive mathematical models of the process were proposed. The first was physical model basing on the identified mechanism of the process. In the second model, artificial neural networks were proposed.

Key words: Bioaccumulation, mechanism, kinetics, mathematical modeling

INTRODUCTION

Bioaccumulation is defined as the transport of pollutants (organic or inorganic) into the cellular interior^[1]. Due to the complexity of the process, the problem lies on the boundary of microbiology, chemistry and bioprocess engineering^{[2],[3]}. Bioaccumulation can find an application only in treatment of effluents containing low level of pollutants (below toxic level for a given organism), containing simultaneously also nutrients (inorganic or organic source of carbon, nitrogen, phosphorus, sulfur etc.)^[4].

The mechanism of heavy metal ions binding and toxic effect caused by them differ between microbial species and heavy metal ions^[5]. Also, chemical nature of pollutants has the fundamental effect on the bioaccumulation process^[6]. Heavy metal ions are usually transported via protein carriers into the cellular interior. The quantity of metal ion transferred into the cellular interior also depends on the concentration of metal ion in the proximity of transporting channel^[7]. The mechanism of bioaccumulation of heavy metal ions by microorganisms is still not understood. The process therefore, has found no practical application so far^{[8],[9],[10]}. There are only few systematic studies in the field of the mechanism, rules, quantitative description of adsorption process and process solutions, while many problems remain unresolved, resulting in limited

industrial application of this method of wastewater treatment^[11].

The idea of the application of microalgae in bioaccumulation of heavy metal ions was proposed many years ago; for the first time by Oswald and Gootas in the year 1957^[12], but this topic has gained attention only recently^{[13],[14]}. Wastewater treatment using living microalgae may also simultaneously eliminate nitrogen and phosphorus compounds that are responsible for eutrophication^{[15],[10]}. In the process of bioaccumulation, the concentration of metal ions may decrease below the level reached in biosorption, although longer time is required^{[16],[17]}.

Literature reports that microalgae are more efficient in heavy metal ions binding than bacteria or fungi^[18]. Probably because the process carried out by living microalgae is associated with metabolic activity and photosynthesis^{[18],[19],[20],[21],[22]}. Microalgae possess high tolerance towards elevated concentration of heavy metal ions. In the presence of these ions, over-expression of specific metal-binding peptides and proteins (i.e. phytochelatins) occurs, that results from their physiological adaptation, since these organisms frequently live in salty environment^{[17],[23],[24]}.

The majority of studies on bioaccumulation of heavy metal ions by microalgae (similarly as the majority of works on bioaccumulation itself) report only the final concentration of metal ions. However,

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only few works provide quantitative kinetic description of the process and investigate its mechanism. The majority of works only report the quantity of metal ions bound by the biomass without quantitative equilibrium and kinetic data, and concern mainly the following microalgal strains: *Chlorella vulgaris*^[25], *Chlamydomonas reinhardtii*^[26] as the model algae^{[9],[18]}.

There are only few models describing bioaccumulation in the literature. The most thoroughly documented was the model elaborated by Prince and Ting^{[11],[27],[28],[29]} that assumed two steps of bioaccumulation process: 1) preliminary, quick binding of metal ions to cellular wall; 2) slower transport through cellular membrane. The suitability of this model was confirmed for the following strains of unicellular algae: *Chlorella pyrenoidosa*, *Chlorella vulgaris* and *Chlamydomonas reinhardtii*.

The aim of the present work was to investigate the mechanism and propose a mathematical description of bioaccumulation process performed by microalgae *Spirulina sp.*, as it was shown previously^[30], that this blue-green alga is suitable for heavy metal ions removal from large volume, diluted effluents via bioaccumulation. Bioaccumulation of Cr(III) ions was studied in typical liquid growth medium in artificially illuminated stirred tank photobioreactor.

MATERIALS AND METHODS

Microorganism and media composition: *Spirulina sp.*, a blue-green alga, obtained from Sigma (USA) was used in this study. *Spirulina* was grown in a photobioreactor (working volume 1 L) at 35°C in Zarrouk liquid medium^[31] containing (g L⁻¹): NaNO₃, 2.50; K₂HPO₄, 0.50; NaHCO₃, 10.00; NaCl, 1.00; MgSO₄·7 H₂O, 0.2; CaCl₂·2 H₂O, 0.02; FeSO₄·7 H₂O, 0.01 enriched with glucose 1.00 and Cr(III) ions (3.1-25.6 mg kg⁻¹) under illumination (32.7 W m⁻²) with photoperiod of 12 hours light and 12 hours dark. Sampling (10 mL) was performed over a period of ca. 100 hours. The construction of the photobioreactor was presented previously^[32].

Analytical methods: All samples were filtered immediately through prewashed and preweighed paper filters (No 2), and cell dry weights were determined after drying filters at 80°C until the samples reached the constant weight. Cell concentration was determined with a UV-160A UV-visible recording spectrophotometer (Shimadzu) at a wavelength of 560 nm (the value independent on pigment concentration). Light intensity was measured with PU 550 Metro Blansko luxmeter. The concentration of Cr(III) ions

was determined by Inductively Coupled Plasma Spectrometry ICP-OES plasma spectrometer (Philips Scientific PU 7000).

Batch bioaccumulation: Cultures were initiated with ca. 0.25 g of *Spirulina* cells in the form of lyophilisate that was used to inoculate the medium (1 L), and grown at 32.7 W m⁻², $c_{Cr(III)}=3.1-25.6$ mg kg⁻¹ 35°C. The culture was aerated with sterilized air (0.1 µm filter) at a flow rate 4.0 mL s⁻¹.

Identification of bioaccumulation mechanism: In order to assess the contribution of passive and active stage of bioaccumulation, as well as to identify the mechanism of the process, the concentration of Cr(III) in the solution, on surface of cells and inside of them was obtained at different interval of time. The suspension of cells (10 mL) was sampled. The cells were removed by centrifugation. Supernatant was analyzed for the content of Cr(III) ions in the solution. The cells were incubated in 5 mL of 0.1 mol L⁻¹ HNO₃ for 5 minutes. It was proved previously^[33] that nitric acid at this concentration enabled to desorb almost all the metal ions bound by the cells without destruction of the biomass. The suspension was then centrifuged. The concentration of metal ions was analyzed in the supernatant. The remaining biomass was used for determination of metal ions concentration inside the cells. The biomass was digested in Microwave Digestion System CEM 2000 (USA) in closed teflon bombs with 5 mL concentrated HNO₃. Under these conditions the cells were completely mineralized. The analysis of post-digestion solutions enabled to assess the total content of metal accumulated in cells. The correctness of this procedure was then confirmed by the mass balance of Cr(III) ions in the system.

Modelling: The parameters of the physical model were determined by *Mathematica* software from Wolfram Research, Inc. The model of artificial neuron network was elaborated with the use of standard procedures included in MATLAB[®] software ver. 7.2 from the MathWorks, Inc.

RESULTS AND DISCUSSION

Mechanism: When discussing the process of bioaccumulation it is necessary to precisely define the subsequent stages. The first step of the process is metal ions binding to the cellular surface. The mechanism of this stage is identical with biosorption and in the present work is described with the term of the *passive* stage of bioaccumulation, since no metabolic activity of

cells was observed. Subsequently, metal ions are transported into the cellular interior (specific bioaccumulation). The process requires energetic expenditures and thus metabolic activity of cells and therefore is described as the *active* stage of bioaccumulation. Bioaccumulation is thus a combination of stages: *passive* and *active*. It is the process that consumes cellular energy for i.e. active transport of metal ions and for cellular growth and synthesis of metal-binding proteins. The consequence is lower process rate and the process is much slower than biosorption alone.

In order to confirm the hypothesis concerning the mechanism of bioaccumulation, the experiment was performed in which metal ions present on the cell surface were distinguished from those, present in its interior. The study was conducted for the initial concentration of Cr(III) ions 25.6 mg kg^{-1} . In this experiment, the quantity of metal ion bound reversibly (in the passive stage) with the biomass (elutable with $0.1 \text{ mol L}^{-1} \text{ HNO}_3$), the quantity of metal ions bound irreversibly (in the active stage) with the biomass (non-elutable with $0.1 \text{ mol L}^{-1} \text{ HNO}_3$), that was determined after biomass digestion with concentrated HNO_3 , as well as metal ions concentration in solution were investigated in time (Fig. 1). Basing on this experiment, it was found that the quantity of metal ions bound with the biomass reversibly (via biosorption) increased during the initial 7 hours, even though biosorption itself is the rapid process, with the equilibrium reached within few minutes. It was possible due to biomass growth and thus the increase of the biomass surface that was available to metal ions. After 7th hour of the process, the quantity of metal ions bound passively decreased, as the result of metabolic activity and the quantity of metal ions bound actively increases. The amount of metal ions bound reversibly decreased below 2 mg/kg after 55 hours. Chromium ions were transported into cellular interior with the simultaneous release of metal ions binding sites on its surface. The quantity of metal ions bound inside the cells increased during the first 55 hours of the process, while the concentration of metal ions in the solution remained unchanged since 30th hour. The process was finished after 55 hours. At this moment metal bound by the biomass was present mainly in its interior, and the surface concentration of metal ions was very low.

Beside the fact that metal ions binding to the cellular surface, similarly as biosorption itself, was the rapid process, ions binding in the passive stage was slower, it endured 7 hours due to biomass growth. However, external metal uptake stabilized during the first several minutes (Fig. 2).

The experiments in which the quantity of metal ions bound to the cellular surface was distinguished from that bound inside the cells were carried out in order to identify the mechanism of bioaccumulation and confirmed preliminary hypothesis that bioaccumulation process consists of two stages:

1. *passive* (biosorption) – rapid stage, lasting for several hours, during which metal ions bind to the surface of cellular wall of microalgae;
2. *active* (adequate bioaccumulation) – stage lasting for tens of hours (in this case ca. 55 hours); in this stage, metal ions were transported into the cellular interior, with the simultaneous release of metal binding sites on cellular surface and binding of the subsequent metal ions as well as metal ions transport. By the end of the process almost all the metal ions were removed from the biomass surface.

When considering the time of conduction of bioaccumulation process, it is necessary to take into account not only metal ions concentration in the solution, but also metal ions concentration on the surface of cells (*passive capacity*). After 24 hours of the process, the concentration of chromium ions in the solution stabilized, but bioaccumulation process was not finished. Metal ions were transported into the cellular interior. After this process had been finished, the passive capacity was low and the biomass could be directly used in another process of metal ions removal as the biosorbent. We assumed that the passive sorption process on the cellular surface is performed in a very similar way in the case of living and non-living cells. However, the active stage of bioaccumulation can be carried out only by living cells.

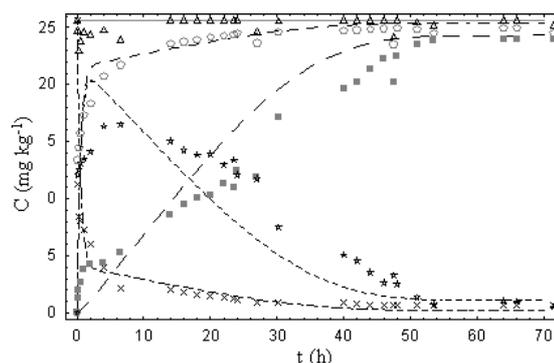


Fig. 1: Location of chromium ions in the process of bioaccumulation, \times - C_{Me} (chromium ions concentration in solution), $+$ - C_{pas} (chromium ions bound in the process of passive biosorption), \blacksquare - C_{act} (chromium ions bound in the process of active bioaccumulation), \circ - $C_{pas} + C_{act}$ (total concentration of metal ions bound with the biomass), \triangle - $C_{Me} + C_{pas} + C_{act}$ (the balance of chromium ions present in the system (in the solution and bound with the biomass)).

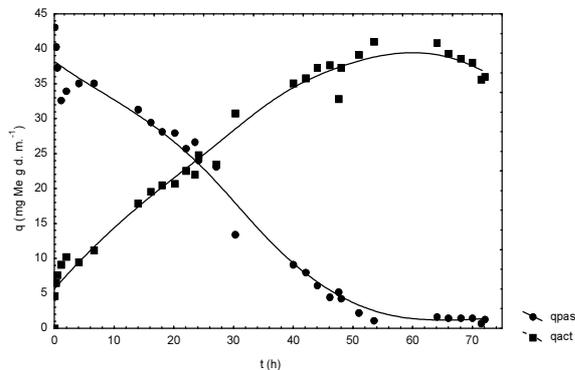


Fig. 2: Metal ions uptake in the passive (q_{pas}) as well as in the active (q_{act}) stage of bioaccumulation.

KINETIC MODELS

Physical model: Generally in bioaccumulation process the following stages, each of different biochemical nature occur. All these processes are associated with mass transfer: sorption to the cellular surface, active transport through cellular membrane into inside of the cells, accumulation inside of the cells.

In the first stage, metal ions present in the solution, are reversibly bound with the free surface of the biomass. The equilibrium between the concentration of metal ions in the solution at the surface of a cell c_{Me} and the concentration of metal adsorbed on its surface c_{pas} can be described with Langmuir equation^[34]:

$$q = \frac{q_{max} \cdot c_{Me}}{1 + b \cdot c_{Me}} \quad (1)$$

for low concentration of metal ions, the above equation can be simplified to the following linear dependence:

$$c_{Me} = a \cdot c_{pas} \quad (2)$$

where a is dimensionless adsorption coefficient and c_{pas} is the concentration of Cr(III) ions adsorbed on the surface on the biomass.

In the second stage, metal ions adsorbed on the cellular surface, after binding with the receptor sites on carrier proteins, are transported through cellular membrane. After passing through cellular membrane, metal ions are released to cytoplasm and/or complexed with proteins are transported to organelles where they become accumulated. The presented mechanism of bioaccumulation can be described by three consecutive equilibrium reactions:



where: c_{Me} - concentration of Cr(III) ions in the solution, c_{pas} - concentration of chromium adsorbed on the surface of the biomass, c_{tran} - concentration of chromium bound with carrier proteins, c_{accum} -

concentration of chromium ions accumulated inside the cells.

The model becomes complete after taking into consideration the concentration of cells as the function of time. In the literature, four cases are considered. The most frequently it is assumed that metal is accumulated by living cells without cellular growth, accumulated by living cells in the phase of linear growth, accumulated by cells in logarithmic phase. Growth of cells is described with Monod equation in the case of limiting concentration of substrates. Monod equation was used previously to describe growth rate of cells^[30]:

$$\frac{dX}{dt} = \mu X \quad (4)$$

where X is the concentration of organisms and μ is the specific growth rate. In the case of nutrient limited cultures, the specific growth rate is given by the following expression:

$$\mu = \mu_{max} \cdot \frac{S}{K_S + S} \quad (5)$$

where μ_{max} is the maximum specific growth rate, K_S is a saturation constant and S is the substrate concentration.

Metal ions can have an effect on cellular growth, that could be either stimulating or inhibiting. Since the rate of sorption process is proportional to the surface of cells, and the rate of accumulation inside of cell is proportional to the volume of cells, it is significant to assess the character of biomass growth.

In mathematical description of microbial processes, common practice is to simplify models in order to reduce the number of model parameters. Since bioaccumulation is associated with active transport through cellular membrane and bioaccumulation of chromium ions in cytoplasm is carried out by specific proteins, *de facto* present inside the cells, it was assumed that the rate of these processes might be expressed by a single constant describing the rate of active transport k_{act} .



When proposing a model it is significant to check experimentally which out of postulated reactions are reversible and which could be considered as irreversible under experimental conditions. In order to investigate this, the cells that were bound with metal ions were eluted with $0.1 \text{ mol l}^{-1} \text{ HNO}_3$ (the part of metal ions bound reversibly with the cells) and with concentrated HNO_3 (the quantity of metal ions bound reversibly and irreversibly with the biomass). Therefore we concluded that the stage of metal ions binding to the cellular surface (adsorption) can be assumed as reversible. In the consequence it was assumed that $k_{pas} \gg k_{act}$.

In a hypothetical case, if all Cr(III) ions were removed from the solution, the process of bioaccumulation by *Spirulina sp.* could be assumed as irreversible and non-equilibrium process and the value of k_{-act} would equal zero. This means that the reaction could be written as follows:



It was assumed that biosorption is the first stage of bioaccumulation. Previously, biosorption of Cr(III) ions to *Spirulina sp.* cells was described with the following Langmuir equation^[34]:

$$q = \frac{2.22 \cdot c_{Me}}{1 + 1.62 \cdot c_{Me}} \quad (8)$$

On the basis of microscopic observations it was observed that during microbial growth, the ratio of cellular mass to their surface is constant. The equation of mass balance and kinetic equations describing concentrations of all forms of Cr(III) ions were proposed:

$$c_{Me}(t) + c_{pas}(t) + c_{act}(t) = c_{Me}(t = 0) \quad (9)$$

$$\frac{dc_{Me}}{dt} = -k_{pas} \cdot X(t) \cdot c_{Me}(t) + k_{-pas} \cdot X(t) \cdot c_{pas}(t) \quad (10)$$

$$\frac{dc_{pas}}{dt} = k_{pas} \cdot X(t) \cdot c_{Me}(t) - k_{-pas} \cdot X(t) \cdot c_{pas}(t) - k_{act} \cdot X(t) \cdot c_{pas}(t) + k_{-act} \cdot X(t) \cdot c_{act} \quad (11)$$

$$\frac{dc_{act}}{dt} = k_{act} \cdot X(t) \cdot c_{pas}(t) - k_{-act} \cdot X(t) \cdot c_{act} \quad (12)$$

Microbial growth in the medium containing no Cr(III) ions was described with the following Monod equation^[33]:

$$\mu_{Cr^{3+}} = 0.058 \cdot \frac{S}{0.101 + S} \quad (13)$$

where $\mu_{Cr^{3+}}$ is specific growth rate of cells in the presence of Cr(III) ions.

The effect of Cr(III) ions on biomass growth rate^[33] was assessed previously. The observed decrease of biomass growth rate was described with the following experimental equations:

$$\mu_{Cr^{3+}} = \mu \cdot \left(1 - \frac{c_{Me}}{6.33 + c_{Me}} \right) \quad (14)$$

After substituting the equation (13), the following equation was obtained:

$$\mu_{Cr^{3+}} = 0.058 \cdot \left(\frac{S}{0.101 + S} \right) \cdot \left(1 - \frac{c_{Me}}{6.33 + c_{Me}} \right) \quad (15)$$

Therefore, in the presence of Cr(III) ions in the growth medium, biomass growth can be described with the following dependence:

$$\frac{dX}{dt} = 0.058 \cdot \left(\frac{S}{0.101 + S} \right) \cdot \left(1 - \frac{c_{Me}}{6.33 + c_{Me}} \right) \cdot X \quad (16)$$

The system of equations describing the mass balance in the system can be solved analytically, after the assumption that at the end of the process pseudo-stationary state is reached in which the concentrations c_{Me} , c_{pas} and c_{act} do not undergo further changes. The following equation describes pseudo-stationary state:

$$\frac{dc_{Me}}{dt} = \frac{dc_{pas}}{dt} = \frac{dc_{act}}{dt} = 0 \quad (17)$$

The system of equations for the conditions of pseudo-stationary state, at the end of the process was solved. Two dependencies were obtained:

$$k_{-pas} = 0.8125 \cdot k_{pas} \quad (18)$$

$$k_{-act} = 0.02107 \cdot k_{act} \quad (19)$$

After substitution to the previous equations, we obtained the following system of dependencies:

$$(20)$$

$$\frac{dc_{pas}}{dt} = k_{pas} \cdot X(t) \cdot c_{Me}(t) - 0.8125 \cdot k_{pas} \cdot X(t) \cdot c_{pas}(t) - k_{act} \cdot X(t) \cdot c_{pas}(t) + 0.02107 \cdot k_{act} \cdot X(t) \cdot c_{act} \quad (21)$$

$$\frac{dc_{act}}{dt} = k_{act} \cdot X(t) \cdot c_{pas}(t) - 0.02107 \cdot k_{act} \cdot X(t) \cdot c_{act} \quad (21)$$

The system of equations was solved by *Mathematica* software with the use of non-linear regression method. The obtained equations were very complex, although described experimental results reasonably well.

Due to the complex nature of biochemical processes, in the case of bioaccumulation by *Spirulina sp.*, the assumption of the pseudo-stationary state may not be correct. For this reason, we decided not to impose the linear dependence binding parameters k_{act} with k_{-act} and k_{pas} with k_{-pas} and the above system of equations was described with numerical equations by simultaneous approximation of all four model parameters. The system was solved numerically with self-consisted parameter iteration method. For each iteration, starting parameters were changed with the assessed parameter that brought the lowest error of estimation. The process of parameters bootstrapping is interrupted when a given accuracy of approximation is reached or when the change of neither of model parameters does not improve fidelity of representation. Finally, the following values of the parameters were obtained: $k_{pas} = 5.88 \text{ l (gh)}^{-1}$, $k_{-pas} = 1.39 \text{ l (gh)}^{-1}$, $k_{act} = 0.11 \text{ l (gh)}^{-1}$, $k_{-act} = 0.005 \text{ l (gh)}^{-1}$. Simultaneously, with the use of least squares methods, estimation error was evaluated as 14 %.

Model of artificial neural network: Parallely with the description of bioaccumulation kinetics with the use of the system of kinetic equations, an attempt of system simulation with the use of algorithm of artificial neural network was performed. Contrary to the kinetic model, algorithm of artificial neural network does not require to implement any kinetic equations *a priori*, nor to

assess specific dependencies of the concentration of metal ions during each phase, when compared with the first model. Therefore, methods that use an algorithm of artificial neural network are used in i.e. modelling of non-linear processes in which it is difficult to provide an accurate mathematical equation (or equations) to describe a given process^[35].

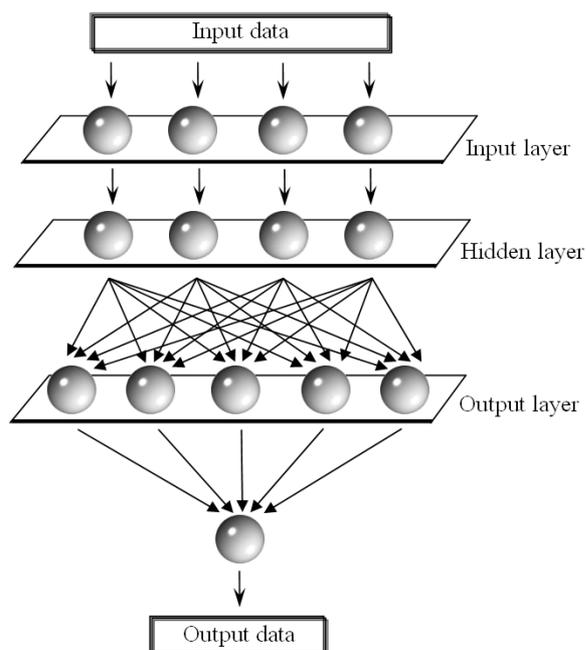


Fig. 3: A representation of a simple 3-layer feedforward artificial neural network with five hidden nodes used in computation of kinetic process.

From over 50 architectures of artificial neural networks^[36] in the simulation, the model of training of neural network with the use of Levenberg-Marquardt algorithm with five neurons in the hidden layer was used (Fig. 3). Experimental data were used as the entrance vector (training vector) for $C_{Cr(III)} = 25.6 \text{ mg kg}^{-1}$. Checking vector (testing vector) was defined basing on data from the studies on mechanism for $C_{Cr(III)} = 19.2 \text{ mg kg}^{-1}$. Unidirectional neural network of backpropagation algorithm was programmed with the use of MATLAB[®] software from MathWorks, assuming that construction of neural network should be finished after the value of goal parameter was below 0.05 or after 5000 training generations. Using testing data, error of estimation with the use of neural method was evaluated as 4.5 %.

CONCLUSIONS

The implemented constants in the proposed kinetic equations are of physical character: k_{pas}

represents the rate of metal ions adsorption to the surface of cells, k_{pas} – the rate of desorption from the cellular surface (passive stage), k_{act} – the rate of active transport of Cr(III) ions from the outside of cells into the cellular interior, k_{act} – the rate of active release of bioaccumulated Cr(III) ions from the inside of the cells into outside.

The constant k_{pas} was significantly higher than the other constants. This means that the process of Cr(III) ions adsorption onto the cellular surface is the quickest stage. The values of k_{pas} represent relatively quick process of elution of Cr(III) ions adsorbed on the cellular surface. The ratio of the constant k_{pas} to k_{act} suggests that the process of active transport to the cellular interior was ca. 50 times slower than the process of surface adsorption. Very low value of k_{act} reflects very low abilities of *Spirulina* to release Cr(III) ions that were previously bioaccumulated. The ratio of k_{pas} to k_{act} furtherly confirms the assumed simplification. It was confirmed that practically only ions adsorbed on the surface of cells were released by elution. The additional advantage of the application of blue-green algae *Spirulina sp.* in bioaccumulation process is that the release of Cr(III) ions, that were bioaccumulated inside of the cell, occurs very slowly.

In the present work two different models were presented: kinetic model and model basing on algorithm of artificial neural network as different approach to describe reaction kinetics. In the first case, kinetic model, that possessed higher error, was proposed. The second model based on the analysis of the process mechanism. The model of artificial neural network however is only the mathematical description, not related with the mechanism of the process. Also, an algorithm of network training is in this case only iteration process of minimization of error function. Additionally, the proposed kinetic model possesses four degrees of freedom, while in an algorithm of artificial neural network five neurons in the hidden layer were used.

Generally an algorithm of artificial neural network can be applied in forecasting evolution of concentration of metal ions in the system during the process, separately from the description of reaction kinetics itself. This type of methods can be applied in interpolation, but frequently it fails in the case of extrapolation. Kinetic model however makes it possible to analyze various aspects of the course of bioaccumulation and can be easily interpreted through the assessment of physical nature of all the constants. Finally, reaction rate constants, determined in the first model might be used to quantitatively assess the applicability of *Spirulina sp.* for the application in

bioaccumulation of Cr(III) ions and modelling that would finally lead to commercial applications.

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