Power-Voltage Characteristics of Power System with the Long Transmission Line

Prechanon Kumkratug
Department of Electrical Engineering, Faculty of Engineering at Si Racha, Kasetsart University, 199 M.6, Tungsukhla, Si Racha, Chonburi, 20230, Thailand

Abstract: Problem statement: Power-Voltage curve provides very important information for voltage stability analysis. The exact long transmission line model consists of the resistance and the reactance. The resistance causes in the active line loss. It is not easy task to achieve the power-voltage curve characteristics of power system with the exact long line model. Approach: This study applies the concept of the Newton-Raphson method to iteratively solve the nonlinear power flow equations. The Power-Voltage (P-V) curve characteristic of the system without line loss and with line loss are plotted and compared on various cases. Results: It is found from the study that the resistance of the line obviously provides the negative effects on the voltage stability. The line loss causes in the decrement of the critical point. In addition, it is found that the leading power factor can increase the critical point of P-V curve. Conclusion: The exact long line model should be considered for voltage stability analysis of the system with the long transmission line.

Key words: Voltage stability, voltage collapse, critical voltage, critical power, power-voltage curve, newton-raphson, reactive power, active power

INTRODUCTION

Power system stability is classified as rotor angle stability and voltage stability. Voltage stability is a stability in power systems which are heavily loaded, disturbance or have a insufficiency of reactive power. Nowadays, the demand of electricity has dramatically increased and a modern power system becomes a complex network of transmission lines interconnecting the generating stations to the major loads points in the overall power system in order to support the high demand of consumers. It is becoming increasingly important to fully utilize the existing transmission system assets due to environmental legislation, rights-of-way issues and costs of construction and deregulation policies that introduced in recent years. A number of Flexible AC Transmission System (FACTS) controllers, based on the rapid development of power electronics technology, have been proposed for better utilization of the existing transmission systems (Omar et al., 2010; Al-Husban, 2009; Osuwa and Igwiro, 2010; Prechanon, 2010; Kumkratug, 2011; Zarate-Minano et al., 2010).

The evaluation of the Power-Voltage (P-V) curve of the power system is one of the most important research areas for power engineers because it indicates the maximum power load. If the load is increased beyond the maximum value, the voltage will be collapsed and then the system is considered as unstable.

The transmission line is one of the most important parts in power system components. Most of the fault occurs at the transmission line. It is generally divided into three major categories; medium, medium and long model whose distance are about 80 km, above 80-250 and above 250 km, respectively. Many previous researches used simple transmission line model by neglecting its resistance or capacitance. To fully utilization the existing system, the exact transmission line should be further investigated.

This study investigated the effects of line loss in long transmission line on voltage stability. The mathematical model of the power flow is systematically derived. The concept of the Newton-Raphson method is applied to iteratively solve the nonlinear power flow equations. The Power-Voltage (P-V) curve characteristic of the system without line loss and with line loss are plotted, discussed and compared on various cases.

MATERIALS AND METHODS

Mathematical model: Consider the simple system with the lump of nominal \( \pi \) model as shown in Fig. 1a. The generator supplies the active power and reactive power, which is transferred through a transmission line to the load. The voltage, active power and reactive power at load are represented by \( V_R \), \( P_R \) and \( Q_R \) respectively.
The voltage at generator bus (V<sub>s</sub>) is considered as constant value. The lump of the nominal π model is represented by an equivalent π model as shown in Fig. 1b.

The equivalent Z' is given by Eq. 1:

\[ Z' = Z_c \sinh \gamma l \]  \hspace{1cm} (1)

The equivalent Y' is given by Eq. 2:

\[ Y' = \frac{2}{Z_c} \sinh \frac{\gamma l}{2} \]  \hspace{1cm} (2)

Here the \( \gamma \) and \( Z_c \) in Eq. 1 and 2 are given by Eq. 3:

\[ \gamma = \sqrt{ZY} / 1 \]  \hspace{1cm} (3)

And:

\[ Z_c = \sqrt{\frac{Z}{Y}} \]  \hspace{1cm} (4)

The constant \( \gamma \) in Eq. 30 and \( Z_c \) are in Eq. 4 the propagation constant and characteristic constant of the long transmission line, respectively. This study applies the concepts of the two ports network to derive power flow at load as given by:

\[ \Lambda = (1 + Y'Z' / 2) \]  \hspace{1cm} (5)

\[ B = Z' \]  \hspace{1cm} (6)

\[ C = Y'(1 + Y'Z' / 4) \]  \hspace{1cm} (7)

\[ D = A \]  \hspace{1cm} (8)

From Eq. 5-8, the voltage and the current at load bus \( (V_R, I_R) \) can be expressed in terms of matrix by

\[
\begin{bmatrix}
V_R \\
I_R
\end{bmatrix} =
\begin{bmatrix}
D & -B \\
-C & A
\end{bmatrix}
\begin{bmatrix}
V_s \\
I_s
\end{bmatrix}
\]  \hspace{1cm} (9)

From Eq. 9, the line current at load bus is given by:

\[ I_R = \frac{V_s - AV_R}{B} = \frac{V_s\angle(\delta - \theta_h)}{B} - \frac{AV_R^2}{B}\angle(\theta_h - \theta) \]  \hspace{1cm} (10)

From Eq. 10, the complex power load is written by:

\[
S_R = P_R + jQ_R = V_R I_R^* = \frac{V_s}{B} \angle(\theta_h - \delta) - \frac{AV_R^2}{B}\angle(\theta_h - \theta_h) \]  \hspace{1cm} (11)

Then the active and reactive power load are given by Eq. 11:

\[ P_R = \frac{V_s V_R}{B} \cos(\theta_h - \delta) - \frac{AV_R^2}{B}\cos(\theta_h - \theta_h) \]  \hspace{1cm} (12)

And:

\[ Q_R = \frac{V_s V_R}{B} \sin(\theta_h - \delta) - \frac{AV_R^2}{B}\sin(\theta_h - \theta_h) \]  \hspace{1cm} (13)
The objective of this study is to evaluate the voltage at load bus ($V_{L}$) with various cases of load. This study applies the Newton-Raphson method to iteratively solve the nonlinear Eq. 12 and 13 given by:

\[
\begin{bmatrix}
\Delta P_{R} \\
\Delta Q_{R}
\end{bmatrix} = 
\begin{bmatrix}
\frac{\partial P_{R}}{\partial \delta} & \frac{\partial P_{R}}{\partial V_{R}} \\
\frac{\partial Q_{R}}{\partial \delta} & \frac{\partial Q_{R}}{\partial V_{R}}
\end{bmatrix}
\begin{bmatrix}
\Delta \delta \\
\Delta V
\end{bmatrix}
\]

(14)

The general form of (14) is given by Eq. 15-17:

\[
\begin{bmatrix}
\Delta P_{R} \\
\Delta Q_{R}
\end{bmatrix} = 
\begin{bmatrix}
J_1 & J_2 \\
J_3 & J_4
\end{bmatrix}
\begin{bmatrix}
\Delta \delta \\
\Delta V
\end{bmatrix}
\]

(15)

Here:

\[
J_1 = \frac{\partial P_{R}}{\partial \delta}
\]

(16)

\[
J_2 = \frac{\partial P_{R}}{\partial V}
\]

(17)

\[
J_3 = \frac{\partial Q_{R}}{\partial \delta}
\]

(18)

\[
J_4 = \frac{\partial Q_{R}}{\partial V}
\]

(19)

RESULTS

The proposed method is tested on the sample system as shown in Fig. 1. The system supplies power which is transferred through a 250 km transmission line to the load. The system voltage at the generator bus is 500 kV. Fig. 2 shows the P-V curve of the system with the long transmission line for various cases of power factor. Table 1 summarizes the critical point ($P_R^c$, $V_R^c$) of Fig. 2.

**DISCUSSION**

It can be seen from the Fig. 2 that without load or light load, the voltage at load is beyond nominal voltage 500 kV because the effect of the shunt line charging. The lagging load provides the negative effects on the voltage stability. As can be seen from the Figure that the lagging load is increased, the voltage at load significantly decreases whereas with the leading power factor, the voltage stability is much better.
REFERENCES


