# **Dynamics of Buses - Part I**

## <sup>1</sup>Relly Victoria Virgil Petrescu, <sup>2</sup>Raffaella Aversa, <sup>1</sup>Gheorghe Frățilă, <sup>3</sup>Taher M. Abu-Lebdeh, <sup>2</sup>Antonio Apicella and <sup>1</sup>Florian Ion Tiberiu Petrescu

<sup>1</sup>ARoTMM-IFToMM, Bucharest Polytechnic University, Bucharest, (CE), Romania <sup>2</sup>Department of Architecture and Industrial Design, Advanced Material Lab, Second University of Naples, 81031 Aversa (CE), Italy <sup>3</sup>North Carolina A and T State University, USA

Article history Received: 02-03-2018 Revised: 02-04-2018 Accepted: 18-04-2018

Corresponding Author: Florian Ion Tiberiu Petrescu ARoTMM-IFTOMM, Bucharest Polytechnic University, Bucharest, (CE), Romania Email: scipub02@gmail.com Abstract: Dynamics, or dynamic processes, is the part of mechanics dealing with the study of processes trying to describe as real as possible the movement of a body, element, mechanism, car, etc., also taking into account the action of the forces on the respective system with their influence on the actual movement of system. The present paper aims to present the study of the dynamics of the vehicles, with particularization on the buses. Here are the main elements of the bus dynamics, taking into account all the elements that influence the dynamic operation of a bus, in general and in particular situations, with emphasis on the main systems and elements that act on the actual, dynamic, on a normal path or on an inclined with an alpha angle path.

Keywords: Mechanisms, Machines, Buses, Dynamics, Kinematics

## Introduction

Transport is the movement of persons as well as goods, signals or information from one place to another. The term comes from Latin, from "transport", trans (over) and porting (meaning wearing or carrying).

Transport is an activity that arose with the existence of man. The physical limits of the human body in terms of walking distances and the quantity of goods that could be transported led, over time, to the discovery of a variety of ways and means of transport.

Transport facilitates access to natural resources and stimulates trade.

The transport sector has different aspects. Simplifying and generalizing can be discussed by three major branches: Infrastructure, vehicles, management:

Transport infrastructure, including the entire transport network (streets, motorways, railways, waterways, flight color, pipelines, etc.) and terminals (airports, railway stations, bus stations, etc.).

Vehicles of all types: Motor vehicles, trains, ships, airplanes, etc., together with all aspects related to vehicle design, construction, diagnosis and exploitation, road traffic, management.

Transport management is the responsibility of transport engineering and engineering for the design of transport networks and systems, aiming at optimizing transport systems, increasing transport safety, protecting the environment, etc.

Land transport is the most widespread form of transport. People can move by their own forces or using means of transport that use human power, such as a bicycle, or they can use animal traction to pull wagons or other types of carriages. The most widespread and efficient form of land transport uses vehicles equipped with liquid-fueled engines (Frățilă et al., 2011; Pelecudi, 1967; Antonescu, 2000; Comănescu et al., 2010; Aversa et al., 2016a; 2016b; 2016c; 2016d; 2017a; 2017b; 2017c; 2017d; 2017e; Mirsayar et al., 2017; Cao et al., 2013; Dong et al., 2013; De Melo et al., 2012; Garcia et al., 2007; Garcia-Murillo et al., 2013; He et al., 2013; Lee, 2013; Lin et al., 2013; Liu et al., 2013; Padula and Perdereau, 2013; Perumaal and Jawahar, 2013; Petrescu and Petrescu, 1995a; 1995b; 1997a; 1997b; 1997c; 2000a; 2000b; 2002a; 2002b; 2003; 2005a; 2005b; 2005c; 2005d; 2005e, 2016a; 2016b; 2016c; 2016d; 2016e; 2013; 2012a; 2012b; 2011; Petrescu et al., 2009; 2016a; 2016b; 2016c; 2016d; 2016e; 2017a; 2017b; 2017c; 2017d; 2017e; 2017f; 2017g; 2017h; 2017i; 2017j; 2017k; 2017l; 2017m; 2017n; 2017o; 2017p; 2017q; 2017r; 2017s; 2017t; 2017u; 2017v; 2017w; 2017x; 2017y; 2017z; 2017aa; 2017ab; 2017ac; 2017ad; 2017ae; Petrescu and Calautit, 2016a; 2016b; Reddy et al., 2012; Tabaković et al., 2013; Tang et al., 2013; Tong et al., 2013; Wang et al., 2013; Wen et al., 2012; Antonescu and Petrescu, 1985; 1989; Antonescu et al., 1985a; 1985b; 1986; 1987; 1988; 1994; 1997; 2000a; 2000b; 2001).



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## **Materials and Methods**

#### Power, Moment and Forces at the Wheels of the Bus

From the engine 1 (Fig. 1), the power is transmitted by the clutch 2, the transaxle 3 of the longitudinal transmission 4 of the main planetary transmission 5 to the drive wheels 6. The effective power On the motor does not reach integral to the wheels of the bus due to the losses occurring in the transmission organs. The power at the wheel  $P_r$  (corresponding to all engine wheels) will be given by relation 1, where the mechanical transmission efficiency is denoted by  $\eta_i$ :

$$P_r = \eta_t \cdot P_e \tag{1}$$

If in relation 1 we introduce instead of the powers their expressions according to the moments and the corresponding angular velocities we obtain in the relational system 2 the moment expression according to the angular velocities, which can also be presented according to the speed, instead of the angular speeds of the motor and respectively of the motor wheels belonging to the bus. Where:  $M_e$  and  $M_r$  are the moments Motor and total wheel respectively in [daN.m],  $\omega$ Angular speed of the motor (motor shaft),  $\omega_r$  Angular speed of the drive wheels in  $[s^{-1}]$ , n The speed of the spindle in [rpm] and the engine speed. The total transmission ratio, between the engine and the engine wheels, is dimensionless.

The  $M_{r'}$  moment returns to a single engine wheel is given by relationship 3, in which *i'* is the number of the motor (driving) wheels of the bus:

$$P_{e} = M_{e} \cdot \omega; P_{r} = M_{r} \cdot \omega_{r};$$

$$\omega = \frac{2\pi \cdot n}{60} = \frac{\pi \cdot n}{30}; i_{t} = \frac{n}{n_{r}}$$

$$P_{r} = \eta_{t} \cdot P_{e} \Longrightarrow M_{r} = M_{e} \cdot \eta_{t} \cdot \frac{\omega}{\omega_{r}}$$

$$M_{r} = M_{e} \cdot \eta_{t} \cdot \frac{n}{n_{r}}$$

$$M_{r} = M_{e} \cdot \eta_{t} \cdot i_{t}$$
(2)

$$M'_r = \frac{M_r}{i} \tag{3}$$

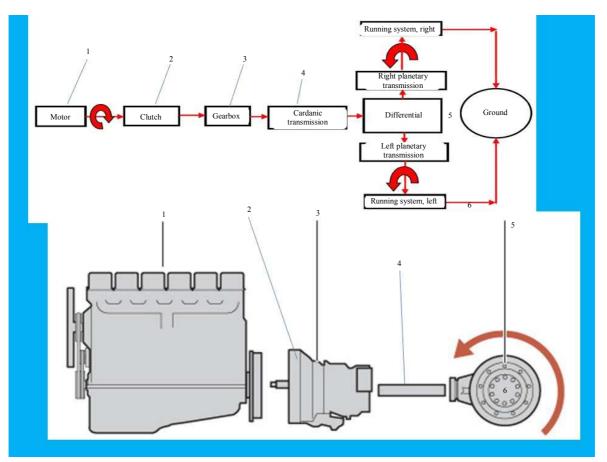


Fig. 1: Scheme of transmission of motion from the engine to the wheels of the bus

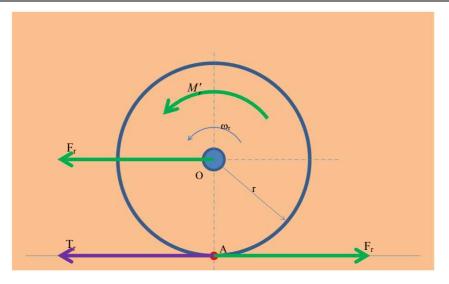


Fig. 2: Moment and forces on an engine (driving) wheel

The total bus transmission ratio is given by relation 4, where  $i_{cv}$  is the transmission ratio of the gearbox,  $i_0$  is the transmission ratio of the main transmission, if the transmission ratio of the final transmission:

$$i_t = i_{cv} \cdot i_0 \cdot i_f \tag{4}$$

The torque  $M'_r$  which returns to a single drive wheel can be replaced by the torque of two forces  $F_r$ applied one in the center O of the bus engine (parallel to the tread) and the second applied at the point Abetween the wheel and a path tangent to A on the wheel circle and on the tread (Fig. 2, relationship 5), where r is the radius of the drive wheel:

$$F_r = \frac{M_r}{r} \tag{5}$$

The  $F_r$  force at the periphery of the drive wheel is called the wheel force. Under the action of force  $F_r$ , the  $T_r$ 's reaction of the rolling path, equal to and opposite to the force  $F_r$ , will be generated, thus preventing the wheel from sliding on the tread. The force  $F_r$  at the center of the wheel is transmitted (via the wheel bearing) to the bus, producing its displacement.

According to the definition, the total pulling force is given by the relation (6):

$$F_{t} = \sum F_{r} = \sum \frac{M'_{r}}{r} = \frac{\sum M'_{r}}{r} = \frac{M'_{r} \cdot i'}{r} = \frac{M_{r}}{r} = \frac{M_{e} \cdot i_{t}}{r} \cdot \eta_{t} \quad (6)$$

The character of the bus movement is given by the force of traction in relation to the size of the resisting forces opposing its displacement.

Knowing the speed of the crankshaft n,  $i_t$  total transmission ratio and the rolling radius of the engine wheels  $r_r$ , can determine the speed of the bus 7:

$$v = r_r \cdot \omega_r = r_r \cdot \frac{\omega}{i_0 \cdot i_{cv} \cdot i_f} = \frac{\pi \cdot n \cdot r_r}{30 \cdot i_0 \cdot i_{cv} \cdot i_f} [ms^{-1}]$$

$$= 0.377 \frac{r_r \cdot n}{i_0 \cdot i_{cv} \cdot i_f} [km / h]$$
(7)

Note: The relationship (7) is valid for as long as clutch slippage and/or some of the bus wheels do not occur.

## Adhesion of Wheels

Under the action of a  $M'_r$  motor torque, a wheel advances only if a tangential reaction  $T_r$  (Fig. 3) is present in the contact point A with the tread that represents the action of the running wheel on the wheel of the bus.

The maximum value of the Trmax tangential response for which there is no slip or sliding of the wheel is called adhesion.

Strength of road, concrete, asphalt, etc. (hard surface) occurs almost entirely by the friction between the wheel tire and the tread. For deformable surfaces, the grip force is due to both the friction and the intersection between the tire protrusions and the track. The more tires are the more desirable the tire-to-rail tire is larger than the theoretical point in the drawing and the adhesion increases but is also resistant to advancing, thus producing greater energy and fuel consumption but also faster wear tires and a more difficult ride, with the clear benefits of increased adherence and enhanced bus comfort (lower vibrations and noise) along with increased dynamic stability.

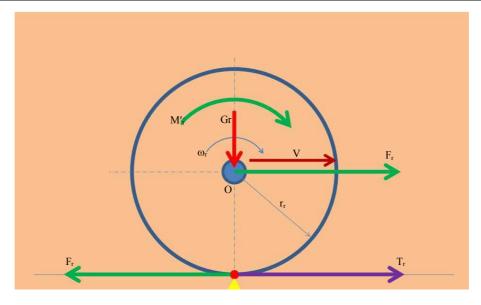


Fig. 3: Forces and reactions to the drive wheel

The ratio of the  $T_{rmax}$  adhesion value to the normal  $Z_r$ of the soil on the wheel is called the coefficient of adhesion to the wheel and is given by the relation (8), where  $\varphi$  is the coefficient of adhesion and  $Z_r$  is the vertical reaction of the rolling path equal to the mobile weight of the  $G_r$  (reversed than this):

$$\varphi = \frac{T_{r\max}}{Z_r} \tag{8}$$

The value of the  $F_{ad}$  adhesion force for all bus wheels of the bus shall be denoted by  $T_{max}$  and shall be equal to their sum (9):

$$T_{\max} = \sum T_{r\max} \equiv F_{ad} \tag{9}$$

For the entire bus, the tractive force  $F_t$  will not exceed the adhesion value for all the engine wheels (10), i.e.:

$$F_t \le T_{\max}, or F_t \le F_{ad} \tag{10}$$

The adhesion coefficient can now be written also according to the total adhesion force  $T_{max}$  corresponding to all the bus wheels of the bus (11), the  $G_{ad}$  being only the part of the weight of the bus allocated to the motor wheels, i.e., a sum of all weights  $G_r$ ; of the relation (11) it is easy to observe that for a given road with the tires already chosen, i.e., for a  $\varphi$  imposed coefficient, it is possible to increase the total adhesion of the  $T_{max}$  bus only by increasing the  $G_{ad}$  force by increasing the number of engine wheels (motor bridges) (12):

$$\varphi = \frac{T_{r\max}}{G_r} = \frac{T_{\max}}{G_{ad}} \tag{11}$$

Way of covering the path	The state of the path	
	Dry	Wet
Paved road	0,7-0,8	0,3-0,4
Cobbled road	0,5-0,6	0,3-0,4
Dirt road	0,5-0,6	0,3-0,4
Sand	0,5-0,6	0,4-0,5
Road covered with snow	0,2-0,4	
Ice Road	0,10-0,15	

Table 1: Average coefficient of adhesion φ

$$T_{\max} = \varphi \cdot G_{ad} \tag{12}$$

The coefficient of adhesion  $\varphi$  depends mainly on the following factors: The nature and condition of the tread, the sliding of the tire and the track, the inner tire pressures, the shape of the tread, the speed of the bus, the total weight and the wheel of the bus, the type of tires and how they were manufactured (here an important role with the materials used).

Table 1 shows the mean coefficient of adhesion  $\varphi$  according to the nature and condition of the tread.

It can be noticed that, while the tread is wet, the coefficient of adhesion decreases drastically (almost half is halved, except for the sand that behaves better in the presence of liquid water). If we have snow, adhesion decreases even more and under the conditions of poll it diminishes dangerously long, having almost no importance of what the road is built, when it is covered by snow or ice.

## Running Ray of the Bus Wheel

The wheels of the current buses (as well as those of the trucks) are equipped with tires that are elastically deformed in the radial, tangential and lateral direction more than for cars or other road vehicles due to the relatively high size of the bus tires but also because of the weight large buses that the wheel and the tire have to bear dynamically. For this reason, they are designed to have a higher elasticity and increased strength and stiffness. As with any other tire-covered vehicle and on buses, the tire's rolling radius and therefore the wheel of the wheel is not a constant one but a variable, dynamic one, the main variation due to the variable dynamic loads it carries permanent.

On a bus wheel the following radii are distinguished: Nominal radius, free radius, static radius, dynamic radius and rolling radius.

The nominal radius of one wheel is the radius of the outer circle of the tire, theoretically deducted by calculation or taken from the tables. The nominal diameters of the bus tires are given in the tables of the international manufacturers, or in the tire standard.

If these tables or chambers are missing, the nominal diameter can be deduced by calculation based on the notations marked on that tire. Based on the tire notation, the nominal radii of the wheels can be calculated. For high pressure tires used on buses, trolleybuses and trucks, the nominal (or external) diameter  $D_e$  (or  $D_u$ ) is marked directly on the tire, the nominal radius being calculated simply by dividing it into two (Fig. 4, top right).

The free radius  $r_0$  of a wheel is the radius of the outer circle of the tire tread at normal pressure, measured without any resting load (Fig. 5a).

The static radius rs of a wheel is defined as the distance between the center of the wheel and the support surface if the wheel is loaded with the normal load and is at rest. The static rays depend primarily on the  $G_r$  load and on the inner tire pressure (Fig 5b).

The dynamic radius of a wheel is defined as the distance between the center of the wheel and the support surface during motion under the action of normal load and torque or tangential force. Under the action of a moment  $M'_r$  will result in a tangential deformation of the tire which results in the center of the wheel being approached by the surface of the tread (Fig. 5c).

The dynamic range of a tire depends on a number of factors: Normal load, torque size, tire pressure, tire material elasticity, etc.

The rolling radius  $r_r$  of a wheel is the radius of a nondeformable conventional wheel running without sliding or skidding at the same rotation speed  $n_r$  and velocity of translation at the center of the wheel (13) where v is the linear displacement velocity of the center real wheel,  $\omega_r$ is the angular velocity of the real wheel but also that of the conventional (calculation) wheel and *n* is the speed of the two wheels (real and conventional):

$$r_r = \frac{v}{\omega_r} = \frac{30 \cdot v}{\pi \cdot n_r} \tag{13}$$

The value of the tread depends on the following factors: The inner tire pressure, the angular speed of the drive wheels, the load on the drive wheel and the rigidity of the tire.

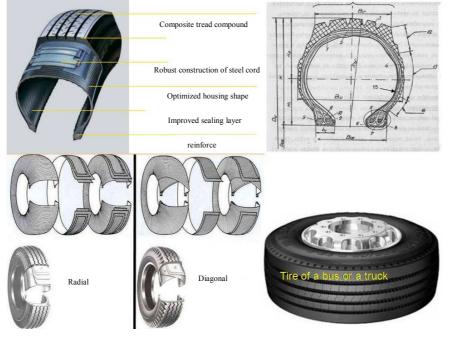


Fig. 4: Tires

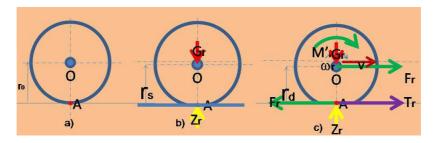


Fig. 5: The free, static and dynamic radius of a bus wheel

For simplification of calculations, the radius of  $r_r$  is usually calculated with relation (14), where  $r_0$  is the free wheel radius, already known and  $\lambda$  is a tire deformation coefficient under the static and dynamic loads, which for tire buses and trolleybuses are between 0.945 and 0.950:

$$r_r = \lambda \cdot r_0 \tag{14}$$

## **Results and Discussion**

#### Mechanical Yield of Transmission

The power of the engine is transmitted to the drive wheels through the motion transmitting organs. During the transmission of power, a part is spent to overcome the friction forces and other resistances that appear in the group of motion transmitting organs.

If it is denoted by  $P_e$  the effective power of the engine and with  $P_{tr}$  the power lost for overcoming all the resistances occurring in the mechanical transmission, then the mechanical efficiency of the transmission is given by relation 15:

$$\eta_t = \frac{P_e - P_{tr}}{P_e} = 1 - \frac{P_{tr}}{P_e}$$
(15)

The lost power  $P_{tr}$  is the sum of the partial losses occurring in the gearbox, in the longitudinal transmission, in the main transmission, in the differential bearings, in the final transmission and in the bearings of the drive wheels.

The mechanical efficiency of the transmission may also be expressed in terms of partial transmission efficiency (relation 16), where  $\eta_{cv}$  is the gearbox efficiency,  $\eta_c$  is the efficiency of the cardanic transmission,  $\eta_0$  represents the efficiency of the main transmission (attack pinion plus toothed crown) and  $\eta_f$  is the efficiency corresponding to the final transmission (differential):

$$\eta_t = \eta_{cv} \cdot \eta_c \cdot \eta_0 \cdot \eta_f \tag{16}$$

Larger losses generally occur in gear units, but also those in longitudinal transmission (cardan transmission) can be very high if the angle  $\gamma$  between the gearbox output shaft and the drive shaft exceeds 10°. Gear losses are mainly of mechanical nature due to the mechanism itself, but they can also be amplified by a significant increase in friction in transmission couples if the lubricants used are not appropriate. In order to avoid operating problems and additional mechanical losses, the machining of the gears should be as appropriate as possible. In a normal execution, the operating efficiencies are the known classics and in special processing the gearing yields increase significantly. The exact way of determining the gearing yields will be done later in the study of each type of gear (gear coupling) in part.

Hydraulic losses depend on the amount and level of lubricant in the crankcase and its properties. By using a low viscosity lubricant but with good lubrication properties, the hydraulic losses are greatly reduced.

The performance of a gearbox depends primarily on the gear in which it operates, then on the torque and the input speed (engine speed, corresponding to the gearbox input). For a certain viscosity of the gearbox oil, gearbox output decreases when the rpm increases and increases as the torque increases (Fig. 6).

During the operation of the bus the yield tends to decrease in case of inappropriate exploitation. The transmission oils used should not only be appropriate but also be changed periodically, avoiding the prolonged use of an old lubricant, which is composed of more and more metal particles detachable in time from the transmission, plus rubbish and in addition old oils begin to lose their original lubrication capability. The timely change of the lubricant prolongs the life of the aggregate, whether it be an engine, a gearshift, or a differential and increases overall transmission efficiency while producing a reduction in fuel consumption. Extending to service an old lubricant used over normal life immediately results in the drastic increase in fuel consumption of the vehicle and the premature wear of the concerned assembly (engine, gearbox, differential).

Table 2 gives the values of the yields of the various transmission components according to the wheel teeth execution, where  $\gamma$  represents the angle of inclination of the shaft. In the calculations, it is recommended for the mechanical efficiency of the transmission to use the values  $\eta_t = 0.82 \dots 0.90$ . The exact determination of its value can be made after studying separately the yields of each organ involved in the mechanical transmission.

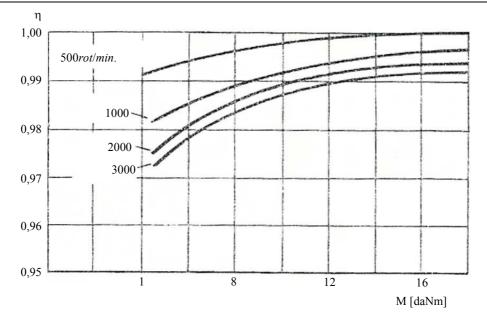


Fig. 6: Variation of gearbox efficiency  $\eta$  (or  $\eta_{cv}$ ) depending on the transmitted M power and the spindle speed n

Table 2: Mechanical transmission efficiency

The element	Normal execution	Special execution
Gearbox		
Direct connection	0,98	0,99
Intermediate connections	0,920,94	0,940,98
Cardanic transmission		
$\gamma = 0 \text{ [deg]}$	1	-
$\gamma = 10 \text{ [deg]}$	0,988	-
$\gamma = 18 \text{ [deg]}$	0,87	-
Main transmision		
Simple, conical, with straight teeth	0,950,96	0,960,98
Simple, conical, with curved teeth	0,900,92	0,930,95
Double	0,920,94	0,940,95

## Resistances to the Bus

Resistance to the bus is a force that opposes its movement. The main resistances for the bus are as follows:

- Resistance to wheel running  $R_r$
- Air resistance  $R_a$
- Resistance to climbing an *R<sub>p</sub>* slope
- Resistance to acceleration *R*<sub>d</sub>

#### *Resistance to Wheel Running R<sub>r</sub>*

Rolling resistance is the force that opposes the movement of the bus and is determined by the losses due to tire and road deformation, the superficial friction between the tire and the road, the friction in the wheel bearings and the wheels and the atmosphere (air) around them.

Figure 7a schematically depicts a deformed tire, under the action of the load  $G_r$  and the moment M', in the course of running on a road considered undeformable. The different elements of the tire (cc', bb', aa') as they enter the required area, suffer radial deformations (compression of the listed segments) and tangential (bending of the segments reached in the requested area).

Figure 7b shows the variation curve of the radial strain  $\Delta r$  depending on the load g that loads the element.

Because of the hysteresis phenomenon, the return curve does not coincide with the deformation curve. The hatched area is proportional to the mechanical work corresponding to the hysteresis losses (due to the internal friction of the material in the area of the deformed elements).

For a deforming element, the radial effort  $g_d$  is greater than the stress  $g_r$  corresponding to the same element in the equivalent but return position. Due to this, the vertical  $Z_r$  path reaction, considered for the entire contact surface, is displaced before point A with the distance a. By moving the force application point (load on the wheel), a moment of rolling resistance  $M_{RL}$  is generated in the opposite direction wheel rotation (relationship 17):

$$M_{rul} = Z_r \cdot a = G_r \cdot a \tag{17}$$

This torque can be replaced by the torque  $R'_r$  (Fig. 7c, relationship 18), where the force  $R'_r$  applied to the center of the wheel is the rolling resistance and the ratio f = a/rr is the coefficient rolling resistance:

$$R'_{r} = \frac{Z_{r} \cdot a}{r_{r}} = G_{r} \cdot \frac{a}{r_{r}} = G_{r} \cdot f$$
(18)

To maintain the movement, a compensating, pushing force parallel to the path equal to  $R'_r$  needs to be developed at the wheel axle.

Table 3 shows the average values of rolling resistance coefficient f depending on the type and condition of the tread (Frățilă *et al.*, 2011).

The rolling resistance of the bus when traveling in a horizontal path is given by the rolling resistance of all the wheels of the bus (supporting both the motor and the non-motor) and can be calculated with relation 19, where  $G_r$  is the weight corresponding to a wheels and  $G_t$  represents the total weight of the bus:

$$R_r = f \cdot \sum G_r = f \cdot G_t \tag{19}$$

When traveling on an inclined path with an angle  $\alpha$  with respect to the horizontal, the relation for calculating the rolling resistance will take form 20 as the total weight of the bus will still press in the vertical direction and its component that will act perpendicularly to the plane of the rolling will be  $Z_t = G_t .cos \alpha$  (Fig. 8):

$$R_r = f \cdot G_t \cdot \cos \alpha \tag{20}$$

The power consumed to overcome rolling resistance is expressed by the relationship (21):

$$P_{rul} = R_r \cdot v = f \cdot G_t \cdot v \cdot \cos \alpha \tag{21}$$

If  $G_t$  is expressed in [daN] and bus speed v in [m/s], then Prul will be expressed in  $[daN.ms^{-1}]$ .

If we want to express the power in [W],  $1W = 1/9,806 \ [daN.m/s]$  and one  $daN.m/s = 9,806 \ [W]$ , so we can write the relation (22) in the international system, in W, the speed will also be introduced in *SI* i.e., in m/s, but for the weight of the  $G_t$  bus will continue to be used as the daN measurement unit instead of *N*:

$$P_{rul} = 9,806 \cdot R_r \cdot v = 9,806 \cdot f \cdot G_t \cdot v \cdot \cos\alpha \tag{22}$$

In order to keep the same input and output units, but the velocity to enter in km/h instead of m/s, the relationship (22) must be amplified by 1/3.6, or else be divided to 3.6. Thus, the relation (23) is obtained in which the velocity V will be introduced in [km/h], the force  $G_t$  in [daN], but the power Prul will still be obtained in SI, i.e., in [W]

$$P_{rul} = 9,806/3, 6 \cdot R_r \cdot V = 2,724 \cdot f \cdot G_t \cdot V \cdot \cos\alpha$$
<sup>(23)</sup>

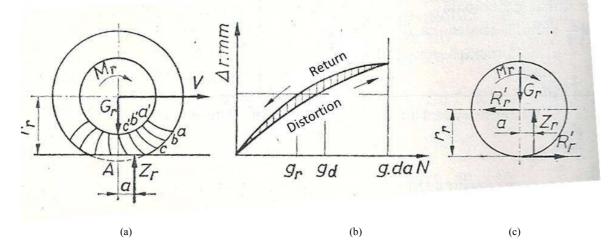


Fig. 7: Resistance to wheel running

Table 3: Average rolling resistance coefficients f

Coefficient of rolling resistance $f$	
0,0120,018	
0,0180,022	
0,0200,025	
0,0250,150	
0,0250,030	
0,1000,300	

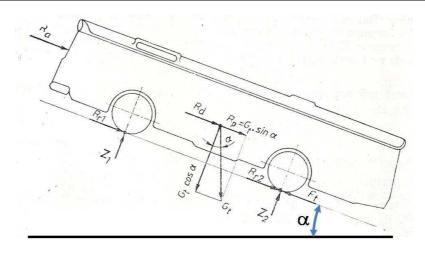


Fig. 8: Traveling the bus in an inclined way with an angle  $\alpha$  to the horizontal

## Conclusion

The present paper aims to present the study of the dynamics of the vehicles, with particularization on the buses. Here are the main elements of the bus dynamics, taking into account all the elements that influence the dynamic operation of a bus, in general and in particular situations, with emphasis on the main systems and elements that act on the actual, dynamic, on a normal path or on an inclined with an alpha angle path.

The paper presents the first part of the bus dynamics.

## Acknowledgement

This text was acknowledged and appreciated by Dr. Veturia CHIROIU Honorific member of Technical Sciences Academy of Romania (ASTR) PhD supervisor in Mechanical Engineering.

## **Author's Contributions**

All the authors contributed equally to prepare, develop and carry out this manuscript.

## Ethics

This article is original and contains unpublished material. Authors declare that are not ethical issues and no conflict of interest that may arise after the publication of this manuscript.

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