

Stochastic Behavior of a Two-Unit Warm Standby System with Two Types of Repairmen and Patience Time

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Abstract: Problem statement: In this study we investigated the probabilistic analysis of a two-unit warm standby system with constant failure rate and two types of repairmen and patience time. The first repairman, usually called regular repairman, always remained with the repair facility, with the known fact that he might not be able to do some complex repairs within some tolerable (patience) time. An expert repairman was called for the system if and only if the regular repairman is unable to do the job, within some fixed time or on system failure, whichever occurs first. **Approach:** Techniques of regenerative point processes had been used to measure the system effectiveness **Results:** The time-dependent availability, steady-state availability, reliability, (MTTF) and profit function were obtained numerically and graphically. **Conclusion:** The availability and profit decreased with respect to the increase of failure rate.

Key words: Availability, busy period, expected number of calls repairman

INTRODUCTION

Reliability is an important concept at the planning design and operation stages of various complex systems. As long as man has been building things, he has wanted to make them as reliable as possible. In this study we investigate the “probabilistic analysis of a two-unit warm standby system with two types of repairmen and patience time”. Although the concept of stochastic behavior of a two-unit cold standby system with two types of repairmen and patience time was discussed by^[4], the concept of two type of failure subject to hardware and human error failures was discussed by^[1], the concept of probabilistic analysis of two unit warm standby system was discussed by^[1,3] and the concept of two-dissimilar unit cold standby redundant system was discussed by^[2]. This study deals with the reliability and availability analysis of system which has two similar units’ one is operative and the other is warm standby. We will introduce the concept of patience time with two types of repairmen for a two unit warm standby system, with different repair rates for regular and expert repairmen. The regular repairman is always available in the repair facility, with the known fact that he might not be able to do some complex repairs within some specified time. The patience time is that for which one can wait while the

regular repairman is undergoing repair for the failed unit. The expert repairman is called to the system when a regular repairman is not able to do some complex repairs. The expert repairman leaves the system after completing the repair of the failed unit and the other unit which fails will be attended first by the regular repairman.

MATERIALS AND METHODS

In this study we analyzed the probabilistic analysis of the system by using of the regenerative processes and have obtained expressions for the various measure of system effectiveness such as the time dependent availability, steady state availability, total fraction of busy period for the regular and expert repairman and total number of visits by the expert repairman per unit time. Using the above measures, profit was calculated. Numerical expression for steady state availability and the profit function were obtained and graphs are also drawn for various parameters involved in the system. We have compared the characteristic, availability and profit with respect to failure rate of the system, to determine when they are improved.

Model description and assumptions: The following assumptions are associated with the model:

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- The system consists of two identical units. Initially one unit is operative and the other unit is warm standby
- Failure of the unit is detected and is attended by the regular repairman
- When failure of a unit is detected, repair of failed unit and switching from the standby starts simultaneously. Switchover is perfect and instantaneous
- System is down when both units are fail
- When the expert repairman is called on to do his job, it takes negligible time to reach the system
- The expert repairman leaves the system after completing repair the failed unit. The other unit which fails will be attended to the regular repairman
- After repair the unit work as good as new
- There is a single repair facility attended by two repairman, (regular and expert)

The system can take one of the following states:

$$S_0(O,ST), S_1(U_r,O), S_2(O,SU_r), S_3(U_e,O), S_4(O,SU_e), S_5(U_r,W_r), S_6(W_r,SU_r), S_7(U_e,W_r), S_8(W_r,SU_e)$$

Where:

- O = The unit is operative
- ST = The unit is standby
- U_r = The operative unit is under regular repairman
- U_e = The operative unit is under expert repairman
- W_r = The unit is waiting for the regular repairman
- SU_r = The stand by unit is under regular repairman
- SU_e = The stand by unit is under expert repairman

RESULTS AND DISCUSSION

Reliability analysis: The equations determining the reliability of the system can be easily obtained from the following:

$$\begin{aligned} R_0(t) &= E_1(t) + E_2(t) \odot R_1(t) + E_3(t) \odot R_2(t), \\ R_1(t) &= E_4(t) + E_5(t) \odot R_0(t) + E_6(t) \odot R_3(t), \\ R_2(t) &= E_8(t) + E_9(t) \odot R_0(t) + E_{10}(t) \odot R_4(t), \\ R_3(t) &= E_{12}(t) + E_{13}(t) \odot R_0(t), \\ R_4(t) &= E_{15}(t) + E_{16}(t) \odot R_0(t) \end{aligned} \quad (1)$$

By using Laplace transform technique, we can solve for $R_0^*(s)$ and is given by:

$$R_0^*(s) = \frac{N(s)}{D(s)} \quad (2)$$

Where:

$$\begin{aligned} N(s) &= E_1^*(s) + E_3^*(s) (E_{10}^*(s)E_{15}^*(s) + E_8^*(s)) + E_2^*(s) (E_6^*(s)E_{12}^*(s) \\ &\quad + E_4^*(s)) \\ D(s) &= 1 - E_3^*(s) (E_{10}^*(s)E_{16}^*(s) + E_9^*(s)) - E_2^*(s) (E_6^*(s)E_{13}^*(s) \\ &\quad + E_5^*(s)) \end{aligned}$$

Availability analysis: We have:

$$A_0(t) = E_1(t) + E_2(t) \odot A_1(t) + E_3(t) \odot A_2(t)$$

The above equation is obtained by considering the two mutually and exhaustive cases:

- No online unit or standby unit fails upon time t
- The online unit fails and hence, the regenerative state 1 occurs
- The standby unit fails and hence, the regenerative state 2 occurs

$$\begin{aligned} A_1(t) &= E_4(t) + E_5(t) \odot A_0(t) + E_6(t) \odot A_3(t) + E_7(t) \odot A_5(t), \\ A_2(t) &= E_8(t) + E_9(t) \odot A_0(t) + E_{10}(t) \odot A_3(t) + E_{11}(t) \odot A_6(t), \\ A_3(t) &= E_{12}(t) + E_{13}(t) \odot A_0(t) + E_{14}(t) \odot A_7(t), \\ A_4(t) &= E_{15}(t) + E_{16}(t) \odot A_0(t) + E_{17}(t) \odot A_8(t), \\ A_5(t) &= E_{18}(t) \odot A_1(t) + E_{19}(t) \odot A_7(t), \\ A_6(t) &= E_{20}(t) \odot A_1(t) + E_{21}(t) \odot A_8(t), \\ A_7(t) &= g_{e1}(t) \odot A_1(t), \\ A_8(t) &= g_{e2}(t) \odot A_1(t) \end{aligned} \quad (3)$$

Using Laplace transform technique, we can solve for $A_0^*(s)$ and is given by:

$$A_0^*(s) = \frac{N_1(s)}{D_1(s)} \quad (4)$$

Where:

$$\begin{aligned} N_1(s) &= A E_1^*(s) + B E_2^*(s) + E_3^*(s) [A (E_8^*(s) + E_{10}^*(s) E_{15}^*(s)) \\ &\quad + B U] \\ D_1(s) &= A - C E_2^*(s) - E_3^*(s) [A (E_9^*(s) + E_{10}^*(s) E_{16}^*(s)) + C U] \end{aligned}$$

With the steady-state availability of the system given by:

$$A_0(0) = \lim_{s \rightarrow 0} s A_0^*(s) = \lim_{t \rightarrow \infty} A_0(t)$$

Busy period analysis for regular repairman: Using the usual definition of $B_i(t)$ for a regular repairman and considering probabilistic arguments, the following recursive relation can be obtained as:

$$\begin{aligned}
 B_0(t) &= E_2(t) \odot B_1(t) + E_3(t) \odot B_2(t), \\
 B_1(t) &= E_4(t) + E_5(t) \odot B_0(t) + E_6(t) \odot B_3(t) + E_7(t) \odot B_5(t), \\
 B_2(t) &= E_8(t) + E_9(t) \odot B_0(t) + E_{10}(t) \odot B_4(t) + E_{11}(t) \odot B_6(t), \\
 B_3(t) &= E_{13}(t) \odot B_0(t) + E_{14}(t) \odot B_7(t), \\
 B_4(t) &= E_{16}(t) \odot B_0(t) + E_{17}(t) \odot B_8(t), \\
 B_5(t) &= E_{22}(t) + E_{18}(t) \odot B_1(t) + E_{19}(t) \odot B_7(t), \\
 B_6(t) &= E_{23}(t) + E_{20}(t) \odot B_1(t) + E_{21}(t) \odot B_8(t), \\
 B_7(t) &= g_{e1}(t) \odot B_1(t), \\
 B_8(t) &= g_{e2}(t) \odot B_1(t)
 \end{aligned} \tag{5}$$

Using Laplace transform technique, we can solve for $B_0^*(s)$ we get:

$$B_0^*(s) = \frac{BE_2^*(s) + E_3^*(s)[A(E_8^*(s) + E_{11}^*(s)E_{23}^*(s)) + U(E_4^*(s) + E_7^*(s)E_{22}^*(s))]}{D_1(s)} \tag{6}$$

The steady-state of idle time of the regular repairman is given by:

$$B_0(0) = \lim_{s \rightarrow 0} s B_0^*(s) = \lim_{t \rightarrow \infty} B_0(t)$$

Busy period analysis for expert repairman: Using the usual definition of $T_i(t)$ for an expert repairman and considering probabilistic arguments, the following recursive relation can be obtained as:

$$\begin{aligned}
 T_0(t) &= E_2(t) \odot T_1(t) + E_3(t) \odot T_2(t), \\
 T_1(t) &= E_5(t) \odot T_0(t) + E_6(t) \odot T_3(t) + E_7(t) \odot T_5(t), \\
 T_2(t) &= E_9(t) \odot T_0(t) + E_{10}(t) \odot T_4(t) + E_{11}(t) \odot T_6(t), \\
 T_3(t) &= E_{12}(t) + E_{13}(t) \odot T_0(t) + E_{14}(t) \odot T_7(t), \\
 T_4(t) &= E_{15}(t) + E_{16}(t) \odot T_0(t) + E_{17}(t) \odot T_8(t), \\
 T_5(t) &= E_{18}(t) \odot T_1(t) + E_{19}(t) \odot T_7(t), \\
 T_6(t) &= E_{20}(t) \odot T_1(t) + E_{21}(t) \odot T_8(t), \\
 T_7(t) &= \bar{G}_{e1}(t) + g_{e1}(t) \odot T_1(t), \\
 T_8(t) &= \bar{G}_{e2}(t) + g_{e2}(t) \odot T_1(t)
 \end{aligned} \tag{7}$$

Using Laplace transform technique, we can solve for $T_0^*(s)$ we get:

$$T_0^*(s) = \frac{LE_2^*(s) + E_3^*(s)(A(E_{10}^*(s)(E_{15}^*(s) + E_{17}^*(s)G_{e2}^*(s)) + E_{11}^*(s)E_{21}^*(s)G_{e2}^*(s)) + L U)}{D_1(s)} \tag{8}$$

The steady-state of idle time of the expert repairman is given by:

$$T_0(0) = \lim_{s \rightarrow 0} s T_0^*(s) = \lim_{t \rightarrow \infty} T_0(t)$$

Expected number of calls for the expert repairman: Using the usual definition the following recursive relation for $V_i(t)$ can be obtained as:

$$\begin{aligned}
 V_0(t) &= E_2(t) \odot V_1(t) + E_3(t) \odot V_2(t), \\
 V_1(t) &= E_5(t) \odot V_0(t) + E_6(t) \odot (1 + V_3(t)) + E_7(t) \odot V_5(t), \\
 V_2(t) &= E_9(t) \odot V_0(t) + E_{10}(t) \odot (1 + V_4(t)) + E_{11}(t) \odot V_6(t), \\
 V_3(t) &= E_{13}(t) \odot V_0(t) + E_{14}(t) \odot V_7(t), \\
 V_4(t) &= E_{16}(t) \odot V_0(t) + E_{17}(t) \odot V_8(t), \\
 V_5(t) &= E_{18}(t) \odot V_1(t) + E_{19}(t) \odot (1 + V_7(t)), \\
 V_6(t) &= E_{20}(t) \odot V_1(t) + E_{21}(t) \odot (1 + V_8(t)), \\
 V_7(t) &= g_{e1}(t) \odot V_1(t), \\
 V_8(t) &= g_{e2}(t) \odot V_1(t)
 \end{aligned} \tag{9}$$

Using Laplace transform technique, we can solve for $V_0^*(s)$ we get:

$$V_0^*(s) = \frac{KE_2^*(s) + E_3^*(s)[A(E_{10}^*(s) + E_{11}^*(s)E_{21}^*(s)) + KU]}{D_1(s)} \tag{10}$$

The steady-state of the expected number of calls for repairman per unit time is given by:

$$V_0(0) = \lim_{s \rightarrow 0} s^2 V_0^*(s) = \lim_{t \rightarrow \infty} \frac{V_0(t)}{t}$$

Profit analysis: Now the expected profit $P(t)$ per unit time incurred to the system is given by:

$$P(t) = C_1\mu_{up}(t) - C_2\mu_r(t) - C_3\mu_e(t) - C_4V_0(t)$$

Where:

- C_1 = The revenue per unit up-time of the system
- C_2 = The cost per unit time for which the regular repairman is busy
- C_3 = The cost per unit time for which the expert repairman is busy
- C_4 = The cost per call for the expert repairman

Where:

$$\begin{aligned}
 A &= 1 - E_7^*(s)(E_{18}^*(s) + E_{19}^*(s)g_{e1}^*(s)) - E_6^*(s)E_{14}^*(s)g_{e1}^*(s) \\
 B &= E_4^*(s) + E_6^*(s)E_{12}^*(s) \\
 C &= E_5^*(s) + E_6^*(s)E_{13}^*(s) \\
 U &= E_{11}^*(s)(E_{20}^*(s) + E_{21}^*(s)g_{e2}^*(s)) + E_{10}^*(s)E_{17}^*(s)g_{e2}^*(s) \\
 L &= E_6^*(s)E_{12}^*(s) + G_{e1}^*(s)(E_6^*(s)E_{14}^*(s) + E_7^*(s)E_{19}^*(s)) \\
 K &= E_6^*(s) + E_7^*(s)E_{19}^*(s)
 \end{aligned}$$

Numerical analysis: the results obtained for the above model are illustrated with numerical example, we assume that $f_i(t) = \lambda_i e^{-\lambda_i t}$, $g_{ji}(t) = \mu_{ji} e^{-\mu_{ji} t}$, $h_i(t) = a_i e^{-a_i t}$, where $i = 1, 2$ $j = r, e$.

Reliability analysis: The mean time to system failure is give by:

$$MTTF = \lim_{s \rightarrow 0} R_0^+(s) = \frac{N(0)}{D(0)}$$

Where:

$$N(0) = (\lambda_1 + \mu_{r1} + a_1)(\lambda_1 + \mu_{r2} + a_2)[(\lambda_1 + \mu_{r2} + a_2)(\lambda_1 + \mu_{e1}) + \lambda_1(\lambda_1 + \mu_{e2}) + \lambda_2(\lambda_1 + \mu_{e1})]$$

$$D(0) = (\lambda_1 + \lambda_2)(\lambda_1 + \mu_{e1})(\lambda_1 + \mu_{e2})(\lambda_1 + \mu_{r1} + a_1)(\lambda_1 + \mu_{r2} + a_2) - \lambda_1(\lambda_1 + \mu_{e2})(\lambda_1 + \mu_{r2} + a_2)(a_1\mu_{e1} + \mu_{r1}(\lambda_1 + \mu_{e1})) - \lambda_2(\lambda_1 + \mu_{e1})(\lambda_1 + \mu_{r1} + a_1)(a_2\mu_{e2} + \mu_{r2}(\lambda_1 + \mu_{e2}))$$

Availability analysis: The time dependent availability of the system is given by:

$$A_0(t) = \frac{\Psi_1}{\prod_{i=1}^8 S_i} + \sum_{i=1}^8 \frac{\Psi_2 e^{S_i t}}{\prod_{r \neq i}^8 S_i(S_i - S_r)}$$

Where:

$$\Psi_1 = \mu_{e2}\mu_{e1}(a_2 + \mu_{r2})(a_1 + \mu_{r1})[((\lambda_1 + \mu_{e1})(a_1 + \mu_{r1}) - a_1\lambda_1)((\lambda_1 + \mu_{e2})(\lambda_1 + \lambda_2 + a_2 + \mu_{r2}) + a_2\lambda_2) + \lambda_1(\lambda_1 + a_1 + \mu_{e1})((\lambda_1 + a_2 + \mu_{r2})(\lambda_1 + \mu_{e2}) + \lambda_2(\lambda_1 + a_2 + \mu_{e2}))]$$

$$\Psi_2 = ((S_i + \mu_{e1})(S_i + \lambda_1 + \mu_{e1})(S_i + a_1 + \mu_{r1})(S_i + \lambda_1 + a_1 + \mu_{r1}) - \lambda_1 a_1 \mu_{e1}(2S_i + \lambda_1 + a_1 + \mu_{r1} + \mu_{e1}) - \lambda_1 \mu_{r1}(S_i + \mu_{e1})(S_i + \lambda_1 + \mu_{e1}))((S_i + a_2 + \mu_{r2})(S_i + \mu_{e2})(S_i + \lambda_1 + \mu_{e2})(S_i + \lambda_1 + a_2 + \mu_{r2}) + \lambda_2(S_i + \lambda_1 + a_2 + \mu_{e2})) + \lambda_1(S_i + \lambda_1 + a_1 + \mu_{e1})(S_i + a_1 + \mu_{r1})((S_i + \lambda_1 + \mu_{e2})(S_i + a_2 + \mu_{r2})(S_i + \lambda_1 + a_2 + \mu_{r2})(S_i + \mu_{e2}) + \lambda_2(S_i + \lambda_1 + \mu_{e2})(\mu_{r2}(S_i + \mu_{e2}) + a_2\mu_{e2}(S_i + a_2 + \mu_{r2})))$$

where, S_i are roots of the polynomial $D_i(s)$ given in Eq. 4.

Busy period analysis for regular repairman: The time dependent busy period for the regular repairman of the system is given by:

$$B_0(t) = \frac{Q_1}{\prod_{i=1}^8 S_i} + \sum_{i=1}^8 \frac{Q_2 e^{S_i t}}{\prod_{r \neq i}^8 S_i(S_i - S_r)}$$

Where:

$$Q_1 = \mu_{e2}\mu_{e1}(a_1 + \mu_{r1})(\lambda_1 + \mu_{e2})(\lambda_1 + a_2 + \mu_{r2})(\lambda_2(a_1\mu_{e1} + \mu_{r1})(\lambda_1 + \mu_{e1}) + (\lambda_1(\lambda_1 + a_1 + \mu_{e1})(a_2 + \mu_{r2})\lambda_1(\lambda_1 + a_1 + \mu_{e1}) + (a_2 + \mu_{r2})\lambda_1\lambda_2(\lambda_1 + \mu_{e1})(a_2 + \mu_{r2})(\lambda_1 + a_2 + \mu_{e2}) + \lambda_2(\lambda_1 + a_1 + \mu_{r1})))$$

$$Q_2 = (S_i + \mu_{e2})(S_i + \lambda_1 + \mu_{e2})(\lambda_1(S_i + a_1 + \lambda_1 + \mu_{e1})(S_i + \mu_{e1})(S_i + a_1 + \mu_{r1})(S_i + a_2 + \mu_{r2})(S_i + \lambda_1 + a_2 + \mu_{r2}) + \lambda_2 X(S_i + a_2 + \mu_{r2})) + \lambda_1 \lambda_2 X$$

Busy period analysis for expert repairman: The time dependent busy period for the expert repairman of the system is given by:

$$T_0(t) = \frac{W_1}{\prod_{i=1}^8 S_i} + \sum_{i=1}^8 \frac{W_2 e^{S_i t}}{\prod_{r \neq i}^8 S_i(S_i - S_r)}$$

Where:

$$W_1 = (a_2 + \mu_{r2})(\lambda_2 a_2 \mu_{e1}(a_1 + \mu_{r1})(\lambda_1 + \mu_{e2})(a_1 \mu_{e1} + \mu_{r1}(\lambda_1 + \mu_{e1})) + \lambda_1 a_1 \mu_{e2}(\lambda_1 + a_2 + \mu_{r1})(\lambda_1 + \lambda_2 + \mu_{e2})(\mu_{e1}(a_1 + \mu_{r1}) + (\lambda_1 + a_1 + \mu_{r1} + \mu_{e1})))$$

$$W_2 = (a_1 \lambda_1 Y((S_i + \mu_{e2})(S_i + \lambda_1 + \mu_{e2})(S_i + a_2 + \mu_{r2})(S_i + \lambda_1 + a_2 + \mu_{r2}) + \lambda_2(a_2 \mu_{e2}(S_i + a_2 + \mu_{r2}) + (S_i + \lambda_1 + \mu_{e2})(a_2 \mu_{e2} + \mu_{r2}(S_i + \mu_{e2}))) + a_2 \lambda_2 X(S_i + a_2 + \mu_{r2})(S_i + \lambda_1 + \mu_{e2})))$$

Expected number of calls for the expert repairman: The number of visits by the expert repairman of the system is given by:

$$V_0(t) = \frac{Z_1}{\prod_{i=1}^8 S_i} + \sum_{i=1}^8 \frac{Z_2 e^{S_i t}}{\prod_{r \neq i}^8 S_i(S_i - S_r)}$$

$$Z_1 = \mu_{e1}\mu_{e2}(a_1\lambda_1(\lambda_1 + \mu_{e1})(\lambda_1 + \mu_{e2})(a_2 + \mu_{r2})(\lambda_1 + a_2 + \mu_{r2})(\lambda_1 + a_1 + \mu_{r1}) + \lambda_2(a_2(a_1 + \mu_{r1})(\lambda_1 + \mu_{e2})(\lambda_1 + a_2 + \mu_{r2})(a_1\mu_{r2} + \mu_{r1}(\lambda_1 + \mu_{e1})) + a_1\lambda_1(a_2 + \mu_{r2})(\lambda_1 + \mu_{e1})(\lambda_1 + a_1 + \mu_{r1})(\lambda_1 + a_2 + \mu_{e2})))$$

$$Z_2 = a_1\lambda_1(S_i + \mu_{e1})(S_i + \mu_{e2})(S_i + \lambda_1 + \mu_{e1})(S_i + \lambda_1 + \mu_{e2})(S_i + a_2 + \mu_{r2})(S_i + \lambda_1 + a_1 + \mu_{r1})(S_i + \lambda_1 + a_2 + \mu_{r2}) + \lambda_2(a_2 X(S_i + \mu_{e2})(S_i + \lambda_1 + \mu_{e2})(S_i + \lambda_1 + a_2 + \mu_{r2}) + \lambda_1 a_1(S_i + \mu_{e1})(S_i + \lambda_1 + \mu_{e1})(S_i + \lambda_1 + a_1 + \mu_{r1})(a_2\mu_{e2}(S_i + a_2 + \mu_{r2}) + (S_i + \lambda_1 + \mu_{e2})(a_2\mu_{r2} + \mu_{r2}(S_i + \mu_{e2}))))$$

Where:

$$X = ((S_i + a_1 + \mu_{r1})(S_i + \mu_{e1})(S_i + \lambda_1 + \mu_{e1})(S_i + \lambda_1 + a_1 + \mu_{r1}) - a_1\lambda_1\mu_{e1}) - \lambda_1(S_i + \lambda_1 + \mu_{e1})(a_1\mu_{e1} + \mu_{r1}(S_i + \mu_{e1}))$$

$$Y = (S_i + \mu_{e1})(S_i + a_1 + \mu_{r1}) + \lambda_1(2S_i + \lambda_1 + a_1 + \mu_{r1} + \mu_{e1})$$

Profit: The expected total profit per unit time incurred to the system in the steady state is given by:

$$P(t) = C_1 A_0 - C_2 B_0 - C_3 T_0 - C_4 V_0$$

Graphical representation:

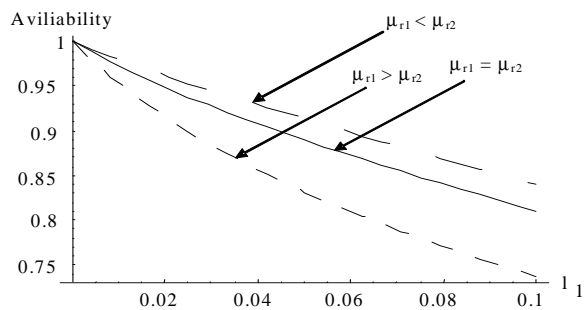


Fig. 1: Relation between availability and λ_1 with various values of μ_{r1}, μ_{r2}

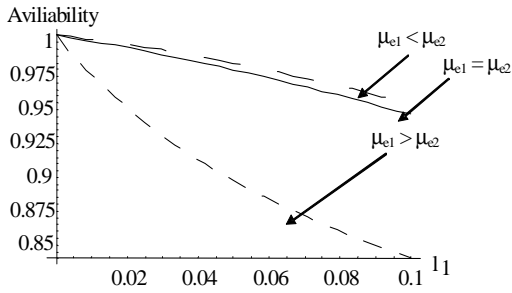


Fig. 2: Relation between availability and λ_1 with various values of μ_{e1}, μ_{e2}

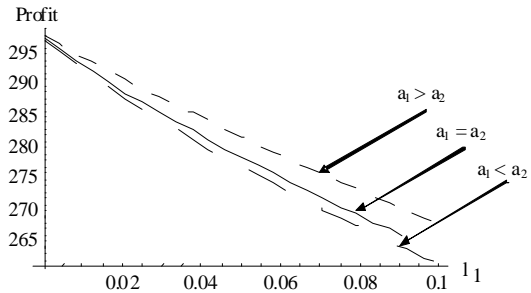


Fig. 6: Relation between profit and λ_1 with various values of a_1, a_2

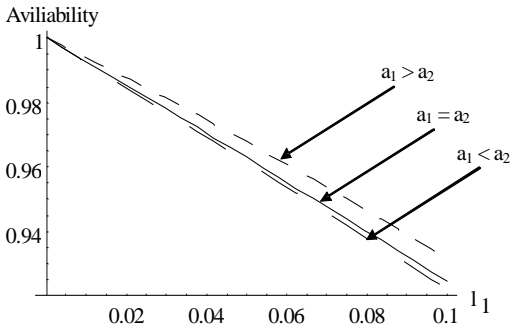


Fig. 3: Relation between availability and λ_1 with various values of a_1, a_2

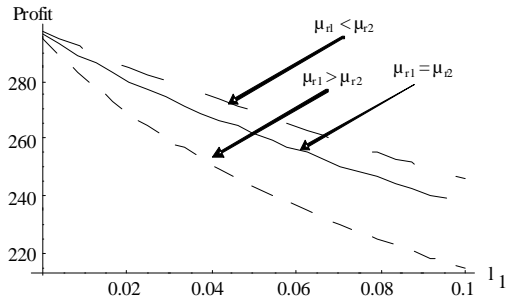


Fig. 4: Relation between profit and λ_1 with various values of μ_{r1}, μ_{r2}

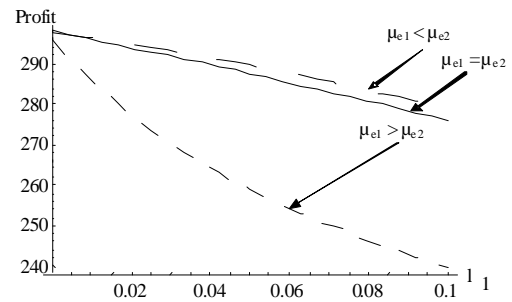


Fig. 5: Relation between profit and λ_1 with various values of μ_{e1}, μ_{e2}

CONCLUSION

By comparing the characteristic, availability and profit with respect to λ_1 for the system at fixed value of λ_2 and various values of $\mu_{r1}, \mu_{r2}, \mu_{e1}, \mu_{e2}, a_1, a_2$ the availability and profit of the system decrease with respect to the increase of λ_1 .

We conclude that the availability and profit are improved when:

- $\mu_{r1} < \mu_{r2}$ than when $\mu_{r1} > \mu_{r2}$ as in Fig. 1 and 4
- $\mu_{e1} < \mu_{e2}$ than when $\mu_{e1} > \mu_{e2}$ as in Fig. 2 and 5
- $a_2 < a_1$ than when $a_2 > a_1$ as in Fig. 3 and 6

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