

Original Research Paper

# Could Geometry Demystify Patterns of Earth Quakes and Aftershocks? An Answer is Yes

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**Abstract:** In this article, a pioneering (geometric) approach based on a new what is named here Glued Bivariate Poisson (GBP) distribution is constructed to demystify the 21st century incidences of earthquakes and their aftershocks. A *warning risk index* for an earthquake or an aftershock to occur is formulated and computed for each of the thirteen major tectonic plates. This article reports a surprise and it is that there exists a *geo angle constancy*, 1.571 in the results pertaining to earthquakes or aftershocks in all the tectonic plates no matter what varying interlocked “*glue level*” among the *African, Antarctica, Arabian, Australian, Caribbean, Coco’s, Eurasian, Indian, North American, Pacific, Philippine, South American and Scotia tectonic plates*. The contents of this article identified higher risk plates, which include *Eurasian, India, Pacific and Philippines plates*, where earthquakes of Kathmandu, Nepal (on 26 April 2015) and Chich-Shima, Japan (on 30 May 2015) occurred as validations of the contents of this article. An interesting geologic-constancy of 1.571 is noticed based on our statistical approach and an appropriate representative random sampling.

**Keywords:** Glued Bivariate Poisson Distribution, Prediction, Correlation, Regression

## Introduction

The earliest earthquake occurred in 1831 BC in the Shandong province of China. The world’s deadliest earthquake occurred in 1556 AD in central China and it killed 830,000 people. The largest earthquake in the world was a magnitude 9.5 in Chile on May 22, 1960. The largest earthquake so far in the United States (USA) occurred with a magnitude 9.2 in Prince William Sound, Alaska on Good Friday, March 28, 1964 UTC. In the year 2011 AD, Japan experienced an earthquake with a magnitude 9.0, which triggered a devastating tsunami. The Tsunami due to an earthquake in Sumatra island of Indonesia on December 26, 2004 killed at least 230,210 people. The 2008 Sichuan earthquake in China’s Sichuan Province in May 2008 resulted in 69,227 fatalities. About 500,000 smaller or larger earthquakes are estimated to occur per year. Many geologists believe that earthquakes above magnitude 7.0 occur only every hundred years. However, there have been an average of 18 *major* earthquakes with magnitude 7.0 through 7.9 and *mega* earthquake with magnitude 8.0 or greater recently. The aftershocks much more than the earthquakes devastate public health killing more humans and destroying more buildings. Scientists wonder

whether earthquakes and/or their aftershocks are more frequent in the 21st century than in the past. If so, such a shift might be due advanced detection and more communication facilities. Let us look in the collected data in <http://en.wikipedia.org>.

First, let us learn the background in the prediction of earthquakes or aftershocks, which occur due to drifting tectonic plates (Wegener, 1912). What is tectonic plate? A German geologist Alfred Wegener announced the breakthrough concept of drifting plate tectonics in 1915 AD in his book *The Origin of Continents and Oceans* based on an observation that the east coast of South America and the west coast of Africa matched. According to Wegener, the lithosphere (the rigid outermost shell of earth), is broken up into eight major tectonic plates and many minor plates. Where the plates meet, their relative motion determines the boundary, which are convergent, divergent, or transform type. Figure 1 for a view of 13 major tectonic plates.

What is an aftershock? An aftershock is a tremor with a smaller magnitude, which occurs after an earthquake. If the magnitude of an *aftershock* is larger than the main earthquake, the aftershock is re-designated as the *main shock* and the original main shock is re-designated as a *foreshock*.



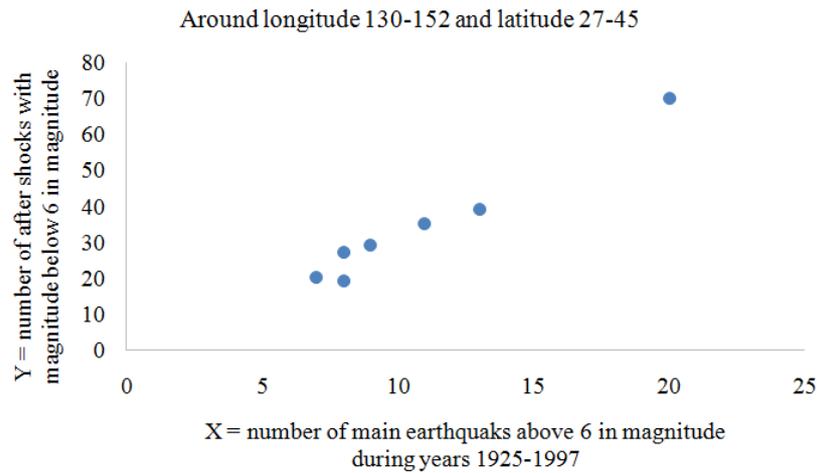


Fig. 2. Glued X, number of earthquakes above 6 magnitude and Y, number of aftershocks

Table 1. Ogata (2001, X = # of shocks > 6 magnitude and Y = # of aftershocks < 6 magnitude within specified *micro region* with longitude and latitude intervals during years 1925-1997

Regional area (longitude, latitude) In degrees	Duration (year 1, year 2)	X = number of main earthquakes Above 6.0	Y = number of aftershocks Below 6.0	Range of aftershock magnitude (min, max) In rector scale
A (142-151, 41-45)	(1982, 1995)	9	29	(3.3, 8.2)
B (140-144, 37-41)	(1928, 1996)	20	70	(0.0, 6.9)
C (137-140, 37-42)	(1939-1995)	7	20	(0.0, 5.3)
D (139-142, 33-37)	(1931-1990)	11	35	(0.0, 5.5)
E (135-139, 35-37)	(1941-1984)	8	19	(0.0, 4.7)
F (134-137, 33-36)	(1925-1995)	8	27	(0.0, 5.5)
G (130-135, 27-36)	(1943-1997)	13	39	(0.0, 5.0)
Correlation $\rho_{(x,y)}$		0.986		

To elaborate this new line of research thinking, a Glued Bivariate Poisson (GBP) distribution with its statistical properties and a geometric methodology based on GBP are introduced in this article. The conceptual and methodological contributions are illustrated using the incidences of earthquake and aftershock in the 21st century in 13 tectonic plates (they are *African, Antarctica, Arabian, Australian, Caribbean, Coco's, Eurasian, Indian, North American, Pacific, Philippine, South American and Scotia plates*). The genius and Nobel laureate Albert Einstein established the fundamental property  $E = MC^2$  where  $E$ ,  $M$  and  $C$  denote respectively the energy, mass and speed of light respectively. Likewise, this article finds a surprise and it is that there exists a *geo angle constancy*, 1.571 in the results pertaining to earthquakes and aftershocks in all the tectonic plates no matter what varying interlocked “glue level” among them.

### Derivation of Glued Bivariate Distribution and its Properties

To be specific, let  $X \geq 0$  and  $Y \geq 0$  be the *number* of earthquakes and aftershocks in a tectonic plate with a

“*geologic glue level*”  $\phi \geq 0$  with its adjacent plates, during a time with incidence rate  $\lambda_1 > 0$  and  $\lambda_2 > 0$  respectively. The earth functions with a chance mechanism, which generates both  $X$  and  $Y$ . This article proposes a candidate to be the underlying distribution for the Random Variable (RV)  $X$  and  $Y$ . It is:

$$p(x, y | \lambda_1, \lambda_2, \phi) = \frac{(1 + \phi xy)}{(1 + \phi \lambda_1 \lambda_2)} [e^{-(\lambda_1 + \lambda_2)} \lambda_1^x \lambda_2^y / x! y!]; \quad (1)$$

$x, y = 0, 1, 2, \dots, \infty; \lambda_1 \geq 0, \lambda_2 \geq 0, \phi \geq 0.$

The Probability Mass Function (PMF) in (1) is named “*glued bivariate Poisson*” distribution. The factor  $1/(1 + \phi \lambda_1 \lambda_2)$  is a *normalizing constant*. Berkhout and Plug (2004) studied a different bivariate Poisson distribution for count data in general.

When the “*geologic glue*” is negligible (that is,  $\phi = 0$ ), the GBP distribution (1) reduces to the product of their marginal probability mass functions  $p(x | \lambda_1) = e^{-\lambda_1} \lambda_1^x / x!$  and  $p(y | \lambda_2) = e^{-\lambda_2} \lambda_2^y / y!$ , implying that the occurrence of an aftershocks is independent of the

occurrence of its earthquakes. If it is the case, the configuration in Fig. 2 ought to have no visible pattern but it did not happen so. Otherwise (that is,  $\phi \neq 0$ ), the occurrence of earthquake is correlated with the occurrence of its aftershocks. This issue needs to be sorted out.

To sort out, we note that:

$$E(XY) = \sum_{x=0}^{\infty} \sum_{y=0}^{\infty} p(x, y | \lambda_1, \lambda_2, \phi) \tag{2}$$

$$= \frac{\lambda_1 \lambda_2 [1 + \phi(1 + \lambda_1)(1 + \lambda_2)]}{(1 + \phi \lambda_1 \lambda_2)}$$

The product moment,  $E(XY)$  is the product,  $\lambda_1 \lambda_2$  of the rate of incidences of the earthquakes and aftershocks, when the tectonic plates are not geologically glued or with a weaker geologic glue level (that is,  $\phi = 0$ ). Otherwise (that is, with a stronger geologic glue level  $\phi \neq 0$ ), the product moment,  $E(XY)$  increases, proportionally to  $\frac{[1 + \phi(1 + \lambda_1)(1 + \lambda_2)]}{(1 + \phi \lambda_1 \lambda_2)}$ . The marginal PMF of the number of earthquakes is:

$$p(x | \lambda_1, \phi) = \sum_{y=0}^{\infty} \left[ \frac{(1 + \phi xy)}{(1 + \phi \lambda_1 \lambda_2)} \right] [e^{-(\lambda_1 + \lambda_2)} \lambda_1^x \lambda_2^y / x! y!]$$

$$= \left[ \frac{(1 + \phi \lambda_2 x)}{(1 + \phi \lambda_1 \lambda_2)} \right] e^{-\lambda_1} \lambda_1^x / x!; \tag{3}$$

$x = 0, 1, 2, \dots, \infty; \lambda_1 \geq 0, \phi \geq 0.$

The *expected value* and the *variance* of the number of earthquakes are respectively:

$$E(X | \lambda_1, \phi) = \sum_{x=0}^{\infty} x p(x | \lambda_1, \phi) \tag{4}$$

$$= [1 + \phi(1 + \lambda_1) \lambda_2] \left( \frac{\lambda_1}{(1 + \phi \lambda_1 \lambda_2)} \right)$$

The Poisson chance mechanism is known to keep no memory of the past patterns and the incidences are rare and sporadic. Johnson *et al.* (1997) for narration of different Poisson chance mechanisms. Likewise, there exists a parallelism with respect to the number of aftershocks. The marginal PMF of the number of aftershocks is:

$$p(y | \lambda_2, \phi) = \sum_{x=0}^{\infty} \left[ \frac{(1 + \phi xy)}{(1 + \phi \lambda_1 \lambda_2)} \right] [e^{-(\lambda_1 + \lambda_2)} \lambda_1^x \lambda_2^y / x! y!]$$

$$= \left[ \frac{(1 + \phi \lambda_1 y)}{(1 + \phi \lambda_1 \lambda_2)} \right] e^{-\lambda_2} \lambda_2^y / y!; \tag{5}$$

$y = 0, 1, 2, \dots, \infty; \lambda_2 \geq 0, \phi \geq 0.$

The *expected value* and the *variance* of the number of aftershocks are respectively:

$$E(Y | \lambda_2, \phi) = \sum_{y=0}^{\infty} y p(y | \lambda_2, \phi) \tag{6}$$

$$= [1 + \phi \lambda_1 (1 + \lambda_2)] \left( \frac{\lambda_2}{(1 + \phi \lambda_1 \lambda_2)} \right)$$

In other words, the role of glue among the tectonics is clear. However, the *covariance* between the number,  $X$  of earthquakes and the number,  $Y$  of aftershocks is:

$$Cov(X, Y) = E(XY) - E(X)E(Y) \tag{7}$$

$$= \frac{\phi \lambda_1 \lambda_2}{(1 + \phi \lambda_1 \lambda_2)^2}$$

Using the product moment,  $E(XY)$  in (2), the marginal moments  $E(X)$  in (4) and  $E(Y)$  in (7). The  $Cov(X, Y)$  in (7) is zero when the tectonic plates are not glued or weakly glued (that is,  $\phi = 0$ ). The covariance increases with a stronger glue level among the tectonic plates. Next, the estimator of the GBP parameters ( $\lambda_1, \lambda_2, \phi$ ) with a bivariate random sample  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$  of size  $n \geq 2$  from the GBP in (1). They are:

$$\hat{\lambda}_{1, \hat{\phi}} \approx \bar{x}(1 + \hat{\phi} \bar{y}) \tag{8}$$

$$\hat{\lambda}_{2, \hat{\phi}} \approx \bar{y}(1 + \hat{\phi} \bar{x}) \tag{9}$$

And:

$$\hat{\phi} \approx \left| \frac{\gamma_{x,y}}{\hat{\lambda}_1 \hat{\lambda}_2 [(1 + \hat{\lambda}_1)(1 + \hat{\lambda}_2) - \gamma_{x,y}]} \right| \tag{10}$$

$$= \left| \frac{\sum_{i=1}^n (x_i y_i - \bar{x} \bar{y})}{\bar{x} \bar{y} [(1 + \bar{x})(1 + \bar{y}) - \sum_{i=1}^n (x_i y_i - \bar{x} \bar{y})]} \right|$$

where,  $\gamma_{x,y}$  denotes the sample *covariance* of between  $x$  and  $y$ . When the *covariance*,  $\gamma_{x,y} = 0$  between the number of earthquakes and the number of aftershocks in a data, the estimate,  $\hat{\phi}$  of the glue level among the tectonic plates is zero. Consequently, the *incidence rate* of earthquakes and aftershocks are respectively the mean  $\bar{x}$  and  $\bar{y}$ . Otherwise (that is, when  $\phi \neq 0$ ), the *incidence rate* of earthquakes and aftershocks increase respectively by a factor of  $(1 + \hat{\phi} \bar{y})$  and  $(1 + \hat{\phi} \bar{x})$ . This article pursues a geometric line of thinking to demystify the uncertainty with respect to the incidences of earthquakes and aftershocks. In the Fig. 3 for the geometric description, the points  $O: (o_1, o_2) = (0,0)$  and  $U: (u_1, u_2) = (1,1)$  denote respectively the location of origin and the location of completion for the probabilities.

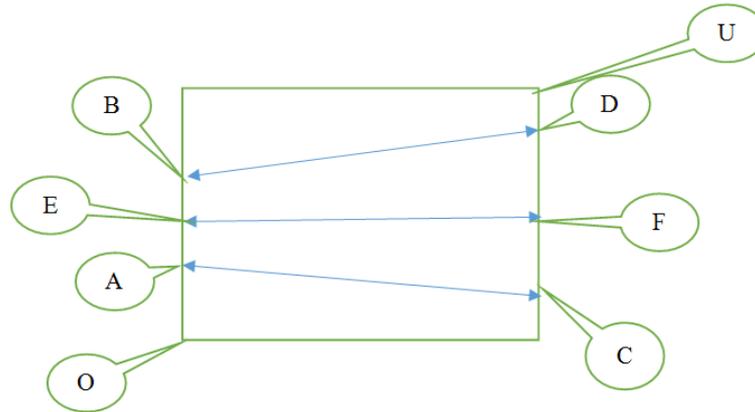


Fig. 3. Trapezoidal chances among no and one earthquake versus no and one aftershock

Let the points  $A: (a_1, a_2) = (0, p_{x,0})$ ,  $B: (b_1, b_2) = (0, p_{y,0})$ ,  $C: (c_1, c_2) = (0, p_{x,1})$  and  $D: (d_1, d_2) = (0, p_{y,0})$  denote the vectors in two dimensional Cartesian coordinates in a mapping (Fig. 3), where:

$$p_{x,0} = \Pr(X=0) = \frac{e^{-\lambda_1}}{(1 + \phi\lambda_1\lambda_2)} \quad (11)$$

$$p_{y,0} = \Pr(Y=0) = \frac{e^{-\lambda_2}}{(1 + \phi\lambda_1\lambda_2)} \quad (12)$$

$$p_{x,1} = \Pr(X=1) = \frac{\lambda_1 e^{-\lambda_1}}{(1 + \phi\lambda_1\lambda_2)} \quad (13)$$

And:

$$p_{y,1} = \Pr(Y=1) = \frac{\lambda_2 e^{-\lambda_2}}{(1 + \phi\lambda_1\lambda_2)} \quad (14)$$

First, note that AB is parallel to CD. Hence, the configuration ABCD is *trapezoid* and it could be *rectangle* if the vector length BD is equal to the vector length AC. In addition, if the vector length AB is equal to the vector length AC, the configuration ABCD is *square*.

The vector length  $AB = \frac{(a_1b_1 + a_2b_2)}{\sqrt{(a_1^2 + a_2^2)(b_1^2 + b_2^2)}}$  denotes a *gap* between the chances of no earthquake and no aftershocks and it is a unit vector (that is,  $AB = 1$ ). In other words, the vector length AB designates an *index of safe period*.

The vector length  $CD = \frac{(1 + p_{x,1}p_{y,1})}{\sqrt{(1 + p_{x,1}^2)(1 + p_{y,1}^2)}}$ , which is clearly not equal to the unit vector  $AB$ , unless  $p_{x,1} = p_{y,1}$  or equivalently there is a *constancy of the earthquake rate and aftershock rate* (that is,  $\lambda_1 = \lambda_2 = \text{constan t}$ ).

What does the *constancy of the earthquake rate and aftershock rate* mean in geological sense? All it means is that the rate of the rare Poisson nature of earthquake events is adapted intact with respect to the rate of tectonic plate's breakup as aftershocks. Does it happen this way in real life? We will examine it in Section 3 with the actual incidences of 21st century.

Furthermore, the ratio  $\mathfrak{R}_{eq} = \frac{CD}{AB}$  indicates an *index level of dilution* of the *constancy of the earthquake rate*. A higher value of the *index level of dilution* means a wider gap between the chances of an earthquake and an aftershock (an alarming period of spectrum) in comparison to the gap between the chances of no earthquake and no aftershock (a safe period of spectrum).

The vector length  $AC = \frac{(a_1c_1 + a_2c_2)}{\sqrt{(a_1^2 + a_2^2)(c_1^2 + c_2^2)}}$  signifies the *risk of earthquake* exiting the comfort zone of no earthquake to uncomfortable zone of experiencing an earthquake and it is  $AC = \frac{p_{x,1}}{\sqrt{(1 + p_{x,1}^2)}}$ . The vector length  $AC$  equals the vector length  $BC$ . The angle  $\text{Cos}(\angle ACB) = \frac{1}{2} \left( 1 - \frac{1}{AC^2} \right)$ . Consequently, the angle of an earthquake incidence is:

$$\theta_{eq} = \angle ACB = \text{Cos}^{-1} \left\{ \frac{1}{2} \left( 1 - \frac{1}{AC^2} \right) \right\} \quad (15)$$

Likewise, the vector length  $BD = \frac{(b_1d_1 + b_2d_2)}{\sqrt{(b_1^2 + b_2^2)(d_1^2 + d_2^2)}}$  signifies the *risk of aftershock* exiting the comfort zone of no aftershock to uncomfortable zone of experiencing an aftershock and it is  $BD = \frac{p_{y,1}}{\sqrt{(1 + p_{y,1}^2)}}$ . The vector length  $AD$  equals the

vector length  $BD$ . The angle  $\text{Cos}(\angle ADB) = \frac{1}{2} \left( 1 - \frac{1}{BD^2} \right)$ . Consequently, the angle of an earthquake incidence is:

$$\theta_{as} = \angle ADB = \text{Cos}^{-1} \left\{ \frac{1}{2} \left( 1 - \frac{1}{BD^2} \right) \right\} \quad (16)$$

The ratio  $\mathfrak{R}_{as} = \frac{BD}{AC}$  indicates an *index level of dilution* of the *constancy of the aftershock rate*. A higher value of the *index level of dilution* means a wider gap between the chances of an earthquake and an aftershock (an alarming period of spectrum) in comparison to the gap between the chances of no earthquake and no aftershock (a safe period of spectrum).

To compare and interpret how the thirteen tectonic plates behave with respect to the risk of both earthquakes and aftershocks, a *percent risk index*:

$$\mathfrak{T} = 100 \left( \frac{\mathfrak{R}_{eq}}{1 + \mathfrak{R}_{eq}} \right) \left( \frac{\mathfrak{R}_{as}}{1 + \mathfrak{R}_{as}} \right) \quad (17)$$

Is worthwhile to compute and display. Larger the risk index  $\mathfrak{T}$  means a higher warning for either earthquake or aftershock or both.

### Illustration of 21st Century Earthquake Incidences and Warnings to Avoid Future Devastations

In this section, the geometric concept to capture and interpret a combined risk level for an earthquake or aftershock in thirteen tectonic plates on earth based on what this article named “glue level” among the tectonic plates. The names of the thirteen tectonic plates are *Antarctica, Arabian, Australia, Caribbean, Cocos, Eurasian, Indian, North American, Pacific, Philippines,*

*South American and Scotia*. The number,  $x$  of earthquakes and the number,  $y$  aftershocks are aggregate of what happened in each major plate and its interlocked adjacent plates. Figure 1 to visualize the names of the adjacent plates for each among the thirteen major plates. All the derived expressions in section 2, based on glued bivariate Poisson distribution are illustrated using earthquakes ( $x$ ) and aftershocks ( $y$ ) incidences during 21st century (see their summary in Table 2 and original data in the webpage <http://en.wikipedia.org>).

It is clear (see  $\rho_{(x,y)}$  Table 2 or the configuration in Fig. 4) that the number of earthquakes and number of aftershocks are correlated. This knowledge suggests that the plates must have been interlocked with some sort of “glue” which would break loose the adjacent plates when an earthquake or aftershock occurs in one plate causing chain reactions. The understanding of the mystery behind the pattern of earthquake or aftershock could be enhanced with a quantified knowledge of the “glue level”,  $\phi \geq 0$ . Using the 21st century data on earthquakes and aftershocks along with the GBP distribution (1) and the estimator (10), the estimates of the “glue” level are obtained and displayed in Table 2. Smaller the “glue” level refers a stronger interlocking among the plates. The “glue” level ranged from 0.01 (in African, Arabian, Indian, North American, Pacific, Philippine plates) to 0.65 (in Scotia plate). The “glue” levels of Australian, Eurasian, Caribbean and South American plates are intermediary.

Using the 21st century data, the estimators (8) and (9), the rate of earthquakes and the aftershocks are obtained, displayed in Table 2 and graphed individually in Fig. 5 and 6 respectively. Clearly, the incidence of earthquake as well as the aftershock declined as the “glue” level is higher. The glue level signifies how strongly the plates are geologically interlocked.

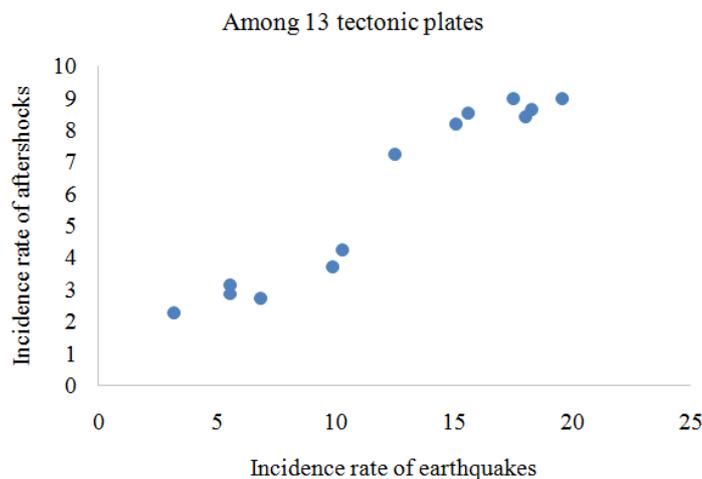


Fig. 4. Pattern between earthquakes and aftershocks

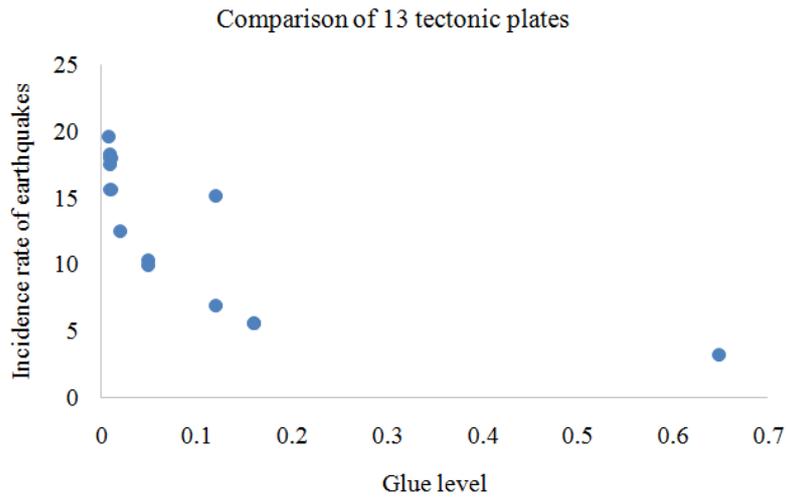


Fig. 5. Relation between the earthquakes and “glue” level

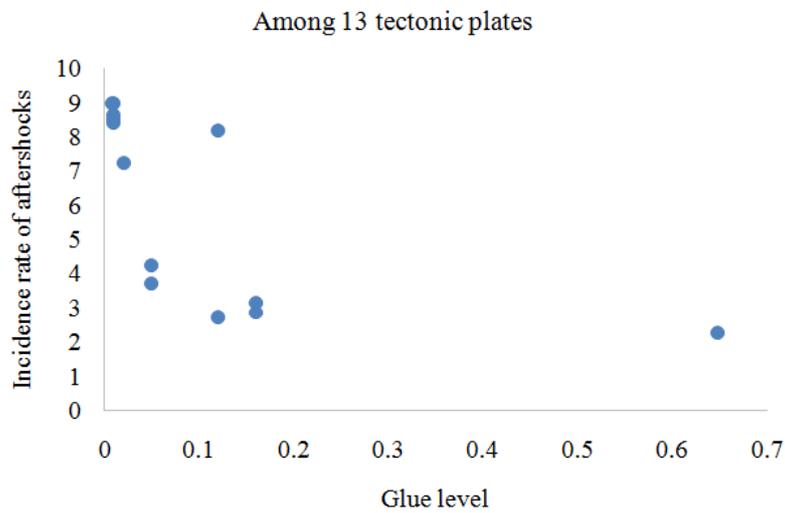


Fig. 6. Relation between aftershocks and the glue level

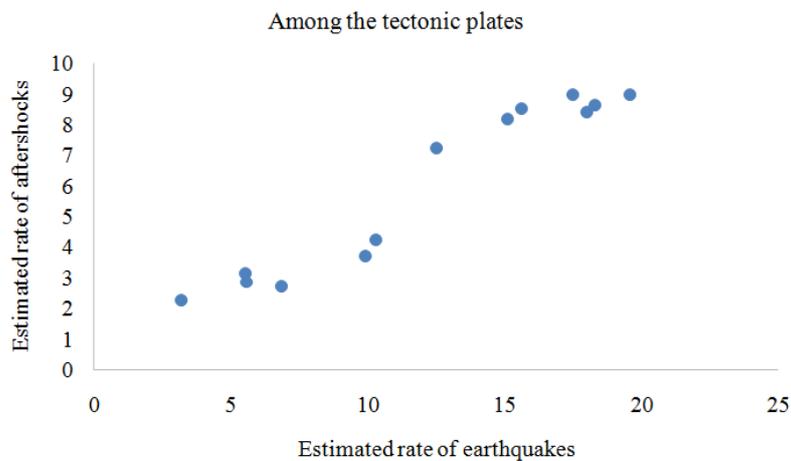


Fig. 7. Relation between the estimated earthquakes and aftershocks

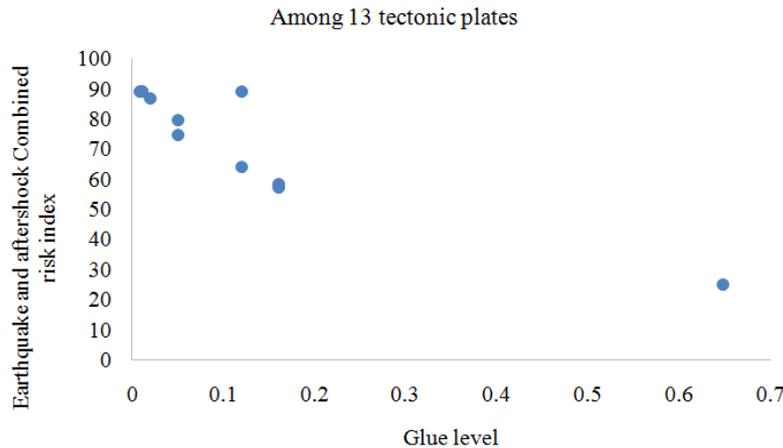


Fig. 8. Combined risk for earthquake or aftershock versus “glue” level

Table 2. A summary of the number (x) of earthquakes and the number (y) of aftershocks in and focused tectonic plates: AN = Antarctica, AR = Arabian, AU = Australia, CA = Caribbean, CO = Cocos, EU = Eurasian, IN = Indian, NA = North American, PA = Pacific, PH = Philippines, SA = South American, ST = Scotia, and their adjacent plates,  $\rho = corr(X, Y)$

Plates	AF	AN	AR	AU	CA	CO	EU	IN	NA	PA	PH	SA	ST
$\rho_{(x,y)}$	0.200	0.200	0.300	0.300	0.700	0.400	0.400	0.200	0.100	0.200	0.300	0.100	0.100
$\hat{\phi}$	0.010	0.050	0.020	0.120	0.160	0.050	0.120	0.010	0.010	0.010	0.010	0.160	0.650
$\hat{\lambda}_1$	15.600	10.300	12.500	6.800	5.600	9.900	15.100	18.300	17.500	19.600	18.000	5.500	3.200
$\hat{\lambda}_2$	8.500	4.200	7.200	2.700	2.800	3.700	8.200	8.600	9.000	9.000	8.400	3.100	2.200
$\mathcal{R}_{eq}$	8.000	4.000	7.000	2.000	2.000	3.000	8.000	8.000	8.000	8.000	8.000	2.000	1.000
$\mathcal{R}_{as}$	643.000	177.000	112.000	24.000	7.000	183.000	553.000	7463.000	2620.000	18407.000	6894.000	6.000	1.000
$\theta_{eq} = \theta_{as} \approx$	1.571	1.571	1.571	1.571	1.571	1.571	1.571	1.571	1.571	1.571	1.571	1.571	1.571
$\mathfrak{S}$	89.000	80.000	87.000	64.000	58.000	75.000	89.000	89.000	89.000	89.000	89.000	57.000	25.000

An intriguing relationship (Fig. 7) between the estimated aftershocks and earthquakes indicates that when one is more the other is also more. Analyzing one without the other is a futile exercise. Every data analysis or predictive warning ought to be done together the earthquakes and aftershocks.

Finally, it is worthwhile to construct a combined warning index for earthquake or aftershock to occur in each major tectonic plate. For this purpose, using the angles ( $\angle ACB$  and  $\angle ADB$ ) in Trapezoid ABDC (Fig. 3 for details) and the data, a warning index,

$$\mathfrak{S} = 100 \left( \frac{\mathcal{R}_{eq}}{1 + \mathcal{R}_{eq}} \right) \left( \frac{\mathcal{R}_{as}}{1 + \mathcal{R}_{as}} \right)$$

for the risk of having an earthquake or aftershock in each major tectonic plate could be constructed and it is summarized in (17). See Table 2 for the estimates of the risk index  $\mathfrak{S}$  in a standardized scale [0, 1]. The risk ranged from 25% (in Scotia plate) to 89% (in African, Eurasian, Indian, North American, Pacific and Philippines plates).

The estimated risk index,  $\mathfrak{S}$  is sketched in terms of the estimated “glue” level of the major tectonic plates in Fig. 8. The pattern reveals an interesting lesson due

to geometric approach that lesser the “glue” level among the adjacent plates refers a higher risk for earthquake or aftershock.

### Conclusion and Comments

No wonder there was a major earthquake (with magnitude 7.3 in Rector Scale) and an aftershock in Kathmandu, Nepal recently on 26 April 2015, as the warning risk index is  $\mathfrak{S} = 89\%$  according to this article. The Eurasian and Indian plates collided on each other while both plates have a risk index of 89% according to the findings of this article. On 30 May 2015 (just two days ago), the location Chichi-Shima, Japan experienced an earthquake with a magnitude 7.8 as its Pacific plate moved beneath the Philippine plate and this article quantified a warning risk index of  $\mathfrak{S} = 89\%$  for both plates. The contents of this article via a geometric approach are validated already by the Kathmandu and Chichi-Shima earthquake incidences. An interesting geologic-constancy of 1.571 is noticed based on our statistical approach and an appropriate representative random sampling. The geometry does indeed demystify

the pattern of earthquake and aftershocks. There is much more that can be done to fully understand what our beloved mother earth undergoes uninformed manner.

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## Ethics

This article is original and contains unpublished material. The corresponding author confirms that all of the other authors have read and approved the manuscript and no ethical issues involved.

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