

Influence of Boundary Conditions on the Behavior of an Anchored Reinforced Earth Wall

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Abstract: The finite element model is used to simulate the behavior of the full scale instrumented anchored reinforced wall. The validated finite element model is then used to carry out parametric studies to ascertain the influence of the boundary conditions on the behavior of the wall. The boundaries at the crest, facing and base of the wall are varied to study their effects. At the crest of the wall, slope surcharge of various geometrical dimensions are imposed. At the facing of the wall, the boundary is allowed to yield laterally by inserting a compressible geoinclusion at the back face of the wall panels. Meanwhile, at the base, the boundary is allowed to yield vertically by allowing the wall to sit on a compressible foundation soil. The behavior of the wall is determined in terms of the tensile stress distribution developed in the reinforcing bars, the summation of the maximum tension in the reinforcing bars, the summation of the tensions developed at the connection to the facing panels, the lateral movement at the facing and the vertical movement at the base.

Key words: Anchor blocks, computer simulation, instrumentation, reinforced earth

INTRODUCTION

In 1981, the Transport and Road Research Laboratory in United Kingdom patented the Anchored Earth wall, which is another type of reinforced soil system. The major difference between the Reinforced Earth and the Anchored Earth is that the Anchored Earth has anchors attached at the free ends of the reinforcing elements whereas the Reinforced Earth has none. Jones^[1] reports the first application of the Anchored Earth wall. Meanwhile, the application of reinforced soil system similar to Anchored Earth is reported in other parts of the world. For example, the loop-shaped anchor system in Austria, the multi-anchor wall system in Japan and the Nehemiah wall system in Malaysia (see Fig. 1)^[2].

Parallel to the rapid development and application of reinforced soil technique is the availability of the high speed computers with great computing power. This easy availability of powerful computers has spurred the growth in the application and sophistication of the numerical modeling technique. This application of this powerful numerical tool in the study of reinforced soil structures in turn leads to a greater in depth understanding of the behavior of reinforced soil structures. Hence, the cost effectiveness of reinforced

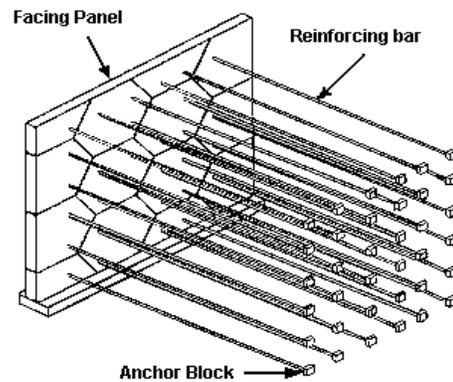


Fig.1: Schematic representation of Nememiah Wall

soil structures coupled with the advent of new materials and high speed computers have resulted in the phenomenal growth in the design, analysis and application of reinforced soil technology throughout the world.

Despite the successive refinements in the design methodology or approach in reinforced earth, the fundamental design philosophy remains the same i.e. it is based on the limit equilibrium method. The basic design assumptions of all these codes and manuals are

that the reinforced soil structure is sitting on a firm ground or piled foundation and that there is little yielding of the lateral boundary. In other words, the present design methodology is unable to take into account the effects of yielding at the base and as well as at the facing of the wall. Hence, if the wall is sitting on a compressible founding soil layer, the present design method is unable to capture the changes in the stresses in the reinforcing elements of the wall as a result of the yielding base. Likewise, if the facing of the wall is allowed to move laterally, the present design method is again unable to capture the changes in the tensile stresses developed in the reinforcing elements due to the lateral yielding. Therefore the main objective of this study was to investigate and determine the influence of the boundary conditions on the behavior of the anchored reinforced wall system. The boundary conditions investigated were the slope surcharge at the crest, the deformation at the facing and the deformation at the base of the wall.

FORMULATION OF FINITE ELEMENT MODEL

The finite element code used was called PLAXIS developed initially in the Technical University of Delft, Netherlands.

The geometry of the finite element model based on the constructed and instrumented Nehemiah wall is shown in Fig. 2. The wall was divided into two tiers. The lower tier was 6.75 m high while the upper tier is 9.0 m high and the total height of the wall was 15.75 m. The upper tier was off set from the lower by 1.5 m. Following the design, the length of the reinforcing bars was 9.9 m long for the bottom two layers while the rest of the bars were 10.9 m long. The vertical spacing of the reinforcing bars was a constant at 0.75 m. The boundaries were sufficiently far away so that they have no significant influence on the behavior of the wall.

Mesh generation: The plot of the finite element mesh is shown in Fig. 2. The mesh was generated by PLAXIS, which had the automatic mesh generation capability. The generation of the mesh was based on a robust triangulation procedure, which resulted in 'unstructured' meshes. These meshes might look disorderly, but the numerical performance of such meshes was usually better than regular (structured) meshes. To ensure reasonably accurate results, the global coarseness was set to medium level. However, for greater accuracy, the meshes between the layers of reinforcing bars were further refined locally. The finite element mesh generated for the analysis of the section

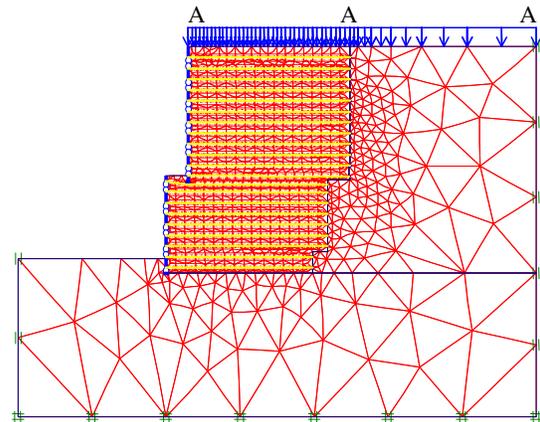


Fig. 2: The geometry of the finite element model

consisted of 1319 elements, 4210 nodes and 3957 stress points.

Boundary conditions: The wall was resting on a firm foundation. The depth of the foundation was truncated at 10 m depth below which the boundary was fixed in both horizontal and vertical direction. The right boundary was fixed in horizontal direction but was allowed to move in the vertical direction. Likewise the left boundary was fixed in horizontal direction but was allowed to move in vertical direction. However, the boundary at the wall facing was allowed to move in both horizontal and vertical direction. The boundary conditions described above are shown in the finite element mesh in Fig. 2.

Initial conditions: After the generation of the finite element mesh, the initial stress state needed to be specified. The initial conditions consisted of two modes namely the generation of initial water pressures and the generation of initial effective stress field. However, for this particular Nehemiah wall, the ground water was well below the base of the founding level and the backfill material was free draining. The water pressure was negligible. The initial stress field was generated for the ground below the founding level because the embankment was constructed subsequently.

Material properties and models: In contrast to the composite model used in the late 70's, the discrete model was used for the present study. In the discrete model, each of the system components was distinctly and separately modeled. The components of the complete model consisted of foundation soil, pad footing, facing panels, backfill material, retained fill, reinforcing bars and the anchor blocks. In addition, soil

structure interaction, the effects compaction and stage construction needed to be considered as well. The properties of each of the components and the modeling techniques involved were discussed below.

Foundation soil: The Mohr-Coulomb soil model was chosen to model the foundation soil. This was an elastic perfectly-plastic soil model. The basic parameters of Mohr-Coulomb model were Young's modulus E' , Poisson's ratio ν' , cohesion intercept c' , friction angle ϕ' and dilatancy angle ψ . From the soil report, it was seen that the foundation soil was firm. The parameters adopted for the foundation soil is shown in Table 1.

The Hardening Soil model is an elastoplastic type of hyperbolic model, formulated in the framework of friction hardening plasticity. It was chosen over the Mohr-Coulomb model for several reasons. Firstly, the Mohr-Coulomb model represents a first order approximation of soil behavior. It is useful for first analysis of problem considered as the computations tends to be very fast. However, the Mohr-Coulomb model allows only a constant value of Young's modulus whereas for real soils, the stiffness is stress dependent. A basic feature of Hardening Soil model is the stress dependency of soil stiffness. Moreover, the Hardening Soil model represents a much more advanced model than the Mohr-Coulomb model. Soil stiffness is described much more accurately by using three different input stiffnesses: the triaxial loading stiffness, E_{50} and the triaxial unloading stiffness. The parameters used for the Hardening Soil model were shown in the Table 2.

The retained fill was normally constructed progressively lift by lift in consonance with the construction of the backfill. The retained fill was made up of material excavated from the original ground, which consisted mainly of residual soil of shale and sandstone origin. It is compacted to 90% Proctor density in lifts of 375 mm thickness. In order to save computing time, the Mohr-Coulomb model was used to model the retained fill. The parameters used for the retained fill is shown in Table 3.

The geoinclusion inserted at the backface of facing panel was made of expanded polystyrene. It had low density 0.15 Kn m^{-3} (0.2 kN m^{-3} was adopted) and low E modulus of 300 kN m^{-2} . It was assumed to behave like the Mohr-Coulomb soil model.

Modeling of concrete components: The concrete components of the system consisted of the facing

Table 1: Material properties of the foundation soil

Parameter	Foundation soil
Material model	Mohr-Coulomb
Type of material behavior	Drained
Dry soil weight γ_{dry} (kN m^{-3})	18
Wet soil weight γ_{wet} (kN m^{-3})	20
Permeability in hor. Direction k_x (m day^{-1})	1
Permeability in vert. direction k_y (m day^{-1})	1
Young's modulus (constant) E_{ref} (kN m^{-2})	80000
Poisson's ratio, ν	0.3
Cohesion (constant) c_{ref} (kN m^{-2})	100
Friction angle, ϕ°	34
Dilatancy angle, ψ°	0
Strength reduction factor inter.	1
Interface permeability	Neutral

Table 2: Material properties of granular backfill

Parameter	Backfill material
Material model	Hardening Soil
Type of material behavior	Drained
Dry soil weight γ_{dry} (kN m^{-3})	18
Wet soil weight γ_{wet} (kN m^{-3})	20
Permeability in hor. Direction, k_x (m day^{-1})	1
Permeability in vert. direction, k_y (m day^{-1})	1
Secant stiffness in standard drained triaxial test E_{50ref} (kN m^{-2})	16000
Tangent stiffness for primary oedometer loading E_{oedref} (kN m^{-2})	16000
Unloading/reloading stiffness E_{ur} (kN m^{-2})	48000
Cohesion, c (kN m^{-2})	100
Friction angle ϕ°	36
Dilatancy angle ψ°	0
Poisson's ratio for unloading/reloading ν_{ur}	0.2
Reference stress for stiffness p_{ref} (kN m^{-2})	100
Power for stress-level dependency of stiffness m	0.5
Ko value for normal consolidation K_{onc}	0.412
Failure ratio q_f/a_a	0.9
Interface strength reduction factor	0.67
Interface permeability	Neutral

Table 3: Material properties of retained fill

Parameter	Retained fill
Material model	Mohr-Coulomb
Type of material behavior	Drained
Dry soil weight γ_{dry} (kN m^{-3})	18
Wet soil weight γ_{wet} (kN m^{-3})	20
Permeability in hor. Direction, k_x (m day^{-1})	1
Permeability in vert. direction, k_y (m day^{-1})	1
Young's modulus (constant), E_{ref} (kN m^{-2})	40000
Poisson's ratio, ν	0.3
Cohesion (constant) c_{ref} (kN m^{-2})	1
Friction angle, ϕ°	30
Dilatancy angle, ψ°	0
Strength reduction factor inter.	1
Interface permeability	Neutral

panels, leveling pad footing and the anchor blocks. They were modeled by beam element which had three nodes when used in conjunction with six-node soil element. The beam element had three degrees of

freedom per node: two translational degrees of freedom (u_x and u_y) and one rotational degree of freedom (rotation in the x-y plane: ϕ_z). They were based on Mindlin's beam theory. This theory allowed for beam deflections due to shearing as well as bending. In addition, the element could change length when an axial force was applied.

Facing panels: The facing panels were normally made of grade 30 precast concrete with nominal reinforcement. Each panel was loosely connected to another by a dowel bar in one panel inserted into the PVC tube embedded in another panel. The joints between the panels were therefore hinged rather than rigid. This hinged connection could be modeled by the beam hinge option available in PLAXIS.

Anchor blocks: The anchor blocks were made of grade 30 concrete. Their sizes were standard block 200×200×100, enlarged blocks 400×200×100 and 600×200×100. As the finite element analysis was based on the plain strain concept, the wall was analyzed based on per linear meter run of wall. However, the blocks were individual isolated blocks separated from each other. An equivalent block of 1 m was determined based on the size and number of blocks per m run of wall. The equivalence was computed based on passive resistance surface area and the flexural stiffness.

Modeling of reinforcing bars: When assessing the suitability of a particular type of model, it is important to consider the behavior of the reinforcing bars. Reinforcing bars are tensile elements, which are able to carry tensile forces but not compressive forces. Although, the bars exhibit a certain degree of stiffness, they generally behave as flexible elements and hence carry negligible bending stresses. The geotextile element exhibits normal stiffness but not bending stiffness. It can only sustain tensile forces but not compressive forces. Neither does it sustain bending stresses. The tensile force distribution along the reinforcing bar can also be displayed. As such, this element is ideally suited to model the reinforcing bar. The only drawback is that the geotextile is a continuous sheet like structure extends in the out-of-plane direction. In contrast, the reinforcing bars are individual bars. Hence, the forces in the bars are converted into equivalent force per m run in the out-of-plane direction before the geotextile element can be used to model the bar. Despite the drawback, geotextile element is found to be the most suitable model for the reinforcing bar.

The effect of compaction on the behavior of retaining wall is significant especially at the upper levels as shown by many researchers^[3,4]. However, the simulation of compaction by the finite element method is not straight forward. Gotteland *et al.*^[5] attempt to simulate the compaction effect by loading and unloading of a uniform surcharge at the top of wall. This similar approach is used by Kim *et al.*^[6] and applied to every soil layer. Due to lack of time and the tedium involved in simulating compaction at every incremental lift, the compaction was simulated at the top of the wall.

The wall was constructed incrementally. Each lift of panel, backfill and reinforcing bars were installed on top of the earlier lift sequentially. This process was repeated layer by layer until the top of the wall was reached. PLAXIS has the option to simulate stage construction. In this option, the configuration of the geometries was changed by deactivating or reactivating cluster or structural objects. Due to the large height of the wall, there are many lifts in the construction sequence. As a result, it is quite tedious to simulate the actual stage construction sequence. Hence, the wall was simulated monotonically instead in this study.

Validation of finite element model: The validation of finite element model was done by comparing the measured results of the Nehemiah wall with the computed results of the finite element model^[2]. The process of validation involved some trial and error and back analysis. For example, initially the Mohr-Coulomb model was used to model the granular backfill. However, to match the order of magnitude of the lateral deformation of the wall facing, the Young's modulus of the soil had to be reduced to a value that is significantly much smaller than the commonly accepted value for granular soil. In fact, it was subsequently found that the Hardening Soil model was a better model in simulating the measured results. The computed and measured results were compared in a number of aspects namely: tensile force distribution along the reinforcing bars (Fig. 3); variation of horizontal pressure with the overburden stress (Fig. 4) and variation of coefficient of lateral pressure with the overburden stress (Fig. 5).

From the above comparison, it was seen that despite some significant discrepancies between the computed and the measured results, the computed results were in general agreement with the measured results. The effects of the compressible layer at the backface of the wall panel were also reasonably well

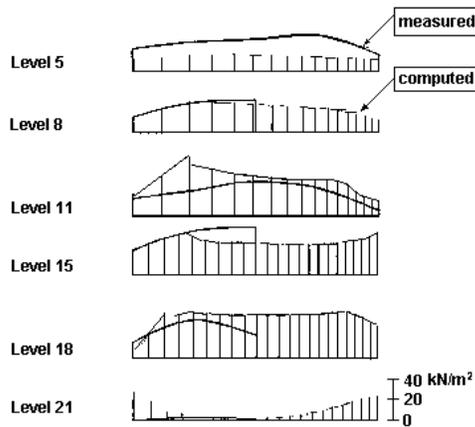


Fig. 3: Computed versus measured results along the reinforcing bars

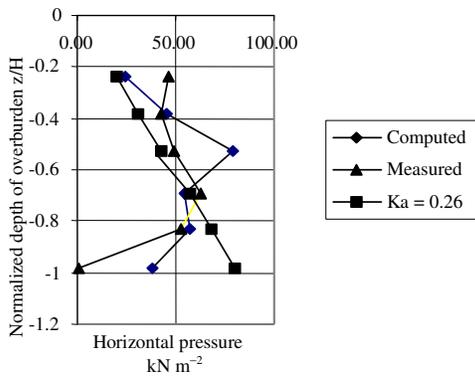


Fig. 4: Variation of horizontal pressure with overburden

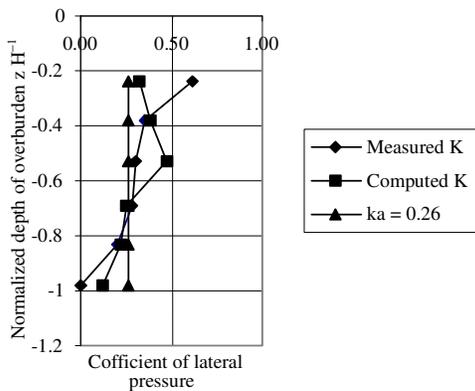


Fig. 5: Variation of coefficient of lateral pressure with overburden

simulated by the finite element modeling. As such, the finite element formulation was suitable to be used for parametric studies to predict the trend and magnitude of the stresses in the reinforcing bars and the deformation characteristics.

INFLUENCE OF LATERAL MOVEMENT AT WALL FACING

The soil at the back face of the wall facing was allowed to move laterally through the introduction of a geoinclusion, which was compressible. In the present parametric study, the compressibility of the geoinclusion as well as its thickness was varied to monitor their effects on the performance of the wall.

Effects of compressibility: The compressibility of the geoinclusion was a function of its E modulus. The E modulus was varied from 300 kN m^{-2} to 5000 kN m^{-2} . The case where there was no geoinclusion was also included for comparison. Where there was no geoinclusion, the maximum tension occurred mostly at the connection. Whereas if the geoinclusion was very compressible that is, where the E modulus was only 300 kN m^{-2} , the tension at connection was only a fraction of the maximum. Andrawes and Saad^[7] report similar behavior for geogrid reinforced walls subjected to controlled lateral deformation. The overall connection ratio Z_{cr} is calculated as follows:

$$Z_{cr} = Z_c/Z_t$$

Where

Z_{cr} is the overall connection ratio

Z_t is the summation of maximum tension in all the reinforcing bars

Z_c is the summation of tension at all connections at the facing

For the case where the E modulus of the geoinclusion was only 300 kN m^{-2} , the overall connection ratio was only 0.30. The variation of the E value versus Z_{cr} is shown in Fig. 6.

The effects of compressibility could further be studied by plotting the horizontal pressures at the connections (i.e. at the backface of the facing panel) against the normalized depth of overburden as shown. From Fig. 7, it was seen that at $E = 300 \text{ kN m}^{-2}$ for the geoinclusion, the horizontal pressure was significantly below the K_a line. Note that the 50E300 means that thickness of the geoinclusion was 50 mm and the E

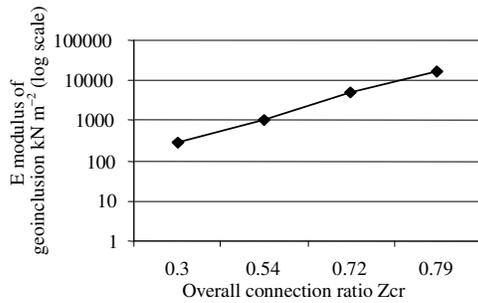


Fig. 6: Effect of compressibility on overall connection ratio

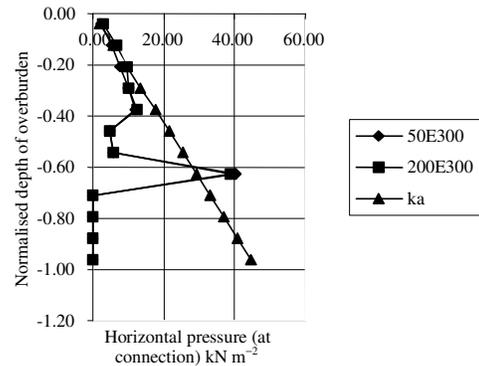


Fig. 8: The effect of the thickness of geoinclusion

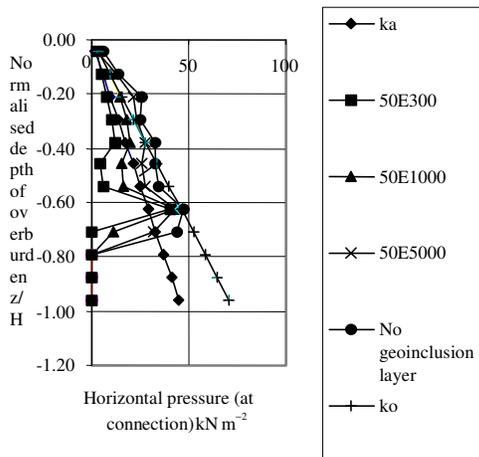


Fig. 7: Horizontal pressure at connection versus depth of overburden

modulus was $300\ kN\ m^{-2}$. When the E value increased to $1000\ kN\ m^{-2}$, the horizontal pressure line followed more or less the K_a line until when the depth of overburden reached $-0.6\ H$ below which the horizontal pressure dropped rapidly to zero. Whereas when there was no geoinclusion, the horizontal pressure line followed more or less the K_o line only until the depth of overburden reached about $-0.7\ H$ below which the horizontal pressure again fall rapidly to zero. It was seen that for all cases, the tension at the connection for the bottom three levels of reinforcing bars was zero.

The above observation was more or less concurred by the findings of Andrawes and Saad^[7] based on studies on 2.1 m high geogrid reinforced experimental walls and finite element modeling using CRISP geotechnical finite element program developed by the University of Cambridge^[8]. Andrawes and Saad^[7] find that the use of geoinclusion at the lateral boundary of the wall results in a significant reduction of the horizontal pressures. The horizontal pressure distribution is found to fall well below the K_a line.

Where there is no geoinclusion in the lateral boundary, the horizontal pressure distribution is significantly above the K_a line until the overburden reaches $-0.7\ H$ below which the horizontal pressure falls below the K_a line.

Effects of thickness of compressible layer: To study the effect of thickness of geoinclusion, the thickness was increased from 50 mm to 200 mm. It was seen from Fig. 8 below that the horizontal pressure lines for both the cases of 50 mm and 200 mm thick geoinclusion more or less coincide. Hence, it could be concluded that the effect of thickness was insignificant. The maximum horizontal displacements of the wall facing were 87.52 mm and 88.23 mm for 50 mm thick and 200 mm thick geoinclusion, respectively. Hence, from deformation point of view, the thickness of geoinclusion was also not significant. However andrawes and Saad^[7] find that the horizontal pressure reduces as the thickness of the geoinclusion increases until the thickness reaches 75 mm beyond which any further increase in thickness would not result in any further reduction in the horizontal pressure. The inability of the PLAXIS to pick up the effects of thickness of the geoinclusion could be due to the relatively small dimension of the thickness compared with the overall height of the wall which is 9 m high. The experimental wall studied by Andrawes and Saad^[7] is only 2.1 m high.

INFLUENCE OF FOUNDATION CONDITION

Effects of compressibility: The effects of compressibility on tension in the reinforcing bars are best seen in the plots shown in Fig. 9. In the figure, the horizontal pressure is plotted against the depth of overburden. It was seen that for the least compressible foundation where $E = 80000\ kN\ m^{-2}$, the maximum

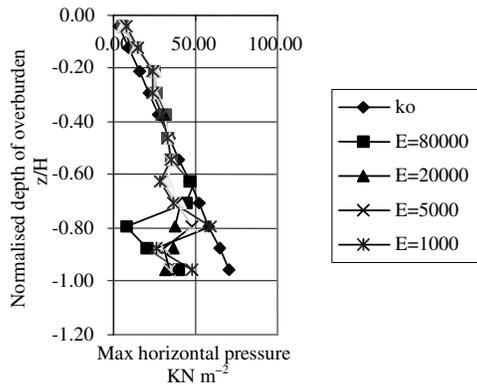


Fig. 9: Plot of maximum horizontal pressure versus depth of overburden

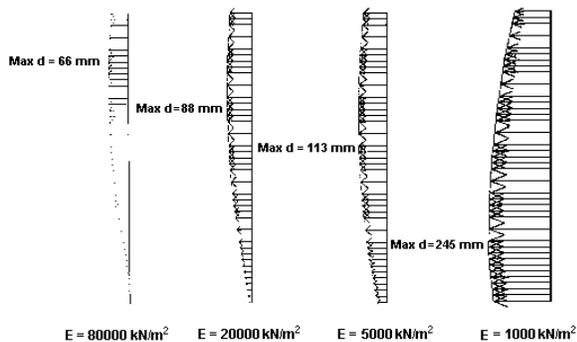


Fig. 10: Horizontal displacement of the wall with varying compressibility of the foundation soil

horizontal pressure occurred at the normalized depth of overburden of 0.6. As the foundation became more compressible i.e. as the E value decreased, maximum horizontal pressure occurred at increasing depth of overburden. When the point of the E value reached 1000 kN m^{-2} , the point of maximum horizontal pressure occurred at a depth of 0.8. In summary, the effect of increasing compressibility was to lower the point of maximum tension from 0.6 to 0.8 of normalized overburden. Putting it in another way, the yielding of the foundation soil tended to redistribute the stress that resulted in larger tensile forces at the lower levels of the reinforcing bars and smaller tensile forces at around 0.6 overburden level. At upper levels that is, where the overburden was less than 0.5 H, the tensile stresses remained unaffected by the compressibility of the foundation soil. The above behavior is consistent with the general understanding that as the foundation soil becomes more compressible, there is more foundation spreading which would result in greater tension at the lower part of the wall.

In Fig. 10 the horizontal displacement of the wall facing is shown for various foundation compressibilities. As the foundation became more compressible, the horizontal displacement increased. The point of maximum displacement moved from the upper part of the wall toward the base of the wall as the foundation became more compressible. Similar trend is reported by Rowe and Ho^[9] whereby forty fold decrease in modulus of foundation soil results in 30% increase in horizontal deformation at the wall face.

CONCLUSION

The above research is carried out to study the influence of boundary conditions on the behavior of Nehemiah wall. The research was done firstly by formulating a finite element model of the wall. The finite element model was then validated by the measured results of the full scale instrumentation of a 15.75 m high Nehemiah wall. With this validated finite element model, parametric studies were carried out by varying the deformation and loading conditions at three boundaries of a 9 m high Nehemiah wall. These three boundaries were the crest, the facing and the base of the wall. The effects of these boundary conditions on the behavior of the wall were evaluated based on certain stress and deformation criteria. The results and conclusions drawn from these studies are summarized below:

At wall facing: As the geoinclusion becomes more compressible, the overall connection ratio Z_{cr} decreases correspondingly. At $E = 300 \text{ kN m}^{-2}$ for the geoinclusion, the Z_{cr} drops to as low as 0.30.

Horizontal pressures at the connection increases with the depth of overburden until a depth of 0.6 H is reached. Beyond 0.6 H, the horizontal pressure starts to reduce with further depth. In the absence of geoinclusion, the horizontal pressure line follow more or less the K_o line until a depth of 0.6H is reached. Below 0.6H the horizontal pressure starts to drop rapidly. With the insertion of the geoinclusion at the wall facing, the horizontal pressure decreases as the geoinclusion becomes more compressible. The influence of the geoinclusion on the horizontal displacement is relatively small. The influence of the thickness of geoinclusion within the range of 50 to 200 mm is not significant.

At base of wall: The increasing compressibility of the foundation soil induces redistribution of stresses that results in larger tensile forces in the reinforcing bars at lower levels and smaller tensile forces at around 0.6 H

depth of overburden. As the foundation becomes more compressible, the horizontal displacement of wall facing increases. The maximum point of horizontal displacement moves from the upper part of the wall facing towards the base as the foundation becomes more compressible.

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