

## Fuzzy Based Energy Management of a Domestic Photovoltaic Panel

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**Abstract:** This study introduces a new switching mean giving a real time optimum connection mode of domestic apparatus on either the electrical grid or a photovoltaic panel (PVP) output. A fuzzy algorithm makes the decision which ensures the optimal energy management basing on the PVP generation and apparatus states with respect to energy save criteria. Validation was driven on a 1kW peak (kWp) PVP and domicile apparatus of different powers installed at the Energy and Thermal Research Centre (CRTEen) in the north of Tunisia. Results confirm that energy save during daylight reaches 90% of the PVP generated energy.

**Key words:** Energy management, fuzzy decision, photovoltaic, energy saves

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### INTRODUCTION

Household electric apparatus have become increasingly diversified during last years, which has led to an increase in energy need. Yet, the energy crisis does not cease being accentuated. These two constraints yield a heavy additional financial expense to the consumer. Several researches have confirmed that more than 60% of total useful energy represents buildings electric energy consumption<sup>[1]</sup>, much of which could be recovered by integrating renewable energy and by formulating adequate energy management strategies inside buildings. For this reason, the exploitation of photovoltaic electricity has become an important issue of debate. Thus, three operating modes of PVP are distinguished: stand alone, grid connected and hybrid mode.

In stand alone mode, the PVP represents the only source of electric energy for equipment. This mode is adopted when the network is not available or when the equipment function depends only on the sun occurrence (pumping, lighting, air-conditioning, heating, etc.). Research interests are essentially related to the modelling<sup>[2-5]</sup>, the optimization<sup>[6]</sup> and the adaptation system<sup>[7]</sup> of the PVP supply according to equipment needs. As for researches carried out on grid connected PVP, they generally deal with system assessment and characterization depending on site climate<sup>[8,9]</sup>. Finally, the hybrid mode is the combination of PVP with other energy sources. Published studies proposed either new design of PVP hybrid energy systems<sup>[10]</sup> or PVP hybrid power systems sizing<sup>[11]</sup>. For all operating modes, other researches developed energy management strategies so as to offer optimum function<sup>[12-14]</sup>. Nevertheless, the main problem in photovoltaic applications remains the battery cost and the protection and synchronization systems of grid connected PVP<sup>[2]</sup> essentially when

using large scale photovoltaic power station.

In this study, a new operating mode is proposed where a domestic PVP is considered as a complementary electric source to supply energy to domestic apparatus. There is no need for batteries neither for grid protection system. The installation incorporates a 1kWp PVP, six apparatus of powers varying between 50W and 500W and a switching unit. A fuzzy decision making algorithm gives orders to the switching unit so as to connect each device either to the PVP output or to the electric grid. The decision of the appropriate connection mode is based on criteria that offer maximum exploitation of the energy delivered by the PVP during daylight depending on load demand without disturbing however apparatus' function. The energy management system is implemented at the Energy and Thermal Research Centre (CRTEen) in the north of Tunisia since January 2005. The results validation is illustrated over four days representing the seasons of the year. Furthermore an energy audit was established and showed that the proposed system is able to bring an energy save during daylight up to 90% of the PVP generated energy.

**The management criteria:** The system studied in the present work aims to offer a utility decision tool on the connection way of domestic apparatus either on a domestic PVP output or on the electric grid. The decision is made in real time on the basis of the following criteria:

- \* To guarantee continuous electric supply for active apparatus.
- \* To minimize the power drawn from the electric grid.
- \* To maximise connection time of PVP connected apparatus so as to avoid relays' commutation.
- \* To reserve a power margin of +10% for each PVP

connected apparatus which guarantees its continuous function face to possible climate perturbation.

- \* To respect apparatus priority: Since an apparatus is connected to PVP output, it has priority to remain connected.
- \* To give apparatus of lower power the higher priority to be connected to PVP output.

The two available sources of electric energy are exploited to provide power for apparatus through fuzzy commands given to apparatus relays with respect of the above decision criteria. Figure 1 traces the synoptic schema of the proposed approach.

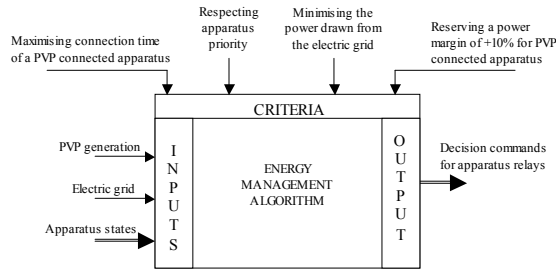


Fig. 1: The synoptic schema of the proposed approach

**The fuzzy management algorithm:** Since the energy management approach uses fuzzy logic, its algorithm is based on three steps: the knowledge base of the expert, the fuzzification and the inference diagram<sup>[16]</sup>.

**The knowledge base of the expert:** The approach handles a multi criteria resolution for which three fuzzy partitions are judged necessary:

**According to apparatus states:** The fuzzy partition of apparatus states is composed of  $N_s = 2$  fuzzy subsets.

$A_{ji} = (\text{OFF}, \text{ON})$  is the  $i^{\text{th}}$  fuzzy subset,  $i = \{1, 2\}$ , of the  $j^{\text{th}}$  apparatus,  $j = \{1, 2, 3, 4, 5, 6\}$ . These subsets cover the fuzzy domain  $X = [0, 1]$  and verify  $\forall x = ER_j \in X, \sum_{i=1}^{N_s} \mu_{A_{ji}}(x) = 1$ , where  $ER_j$  is

the state of the  $j^{\text{th}}$  apparatus and  $\mu_{A_{ji}}$  the membership function.

**According to 1 KWp PVP generation:** Here the fuzzy partition is composed of  $N_s = 20$  fuzzy subsets  $B_l = (A, B, \dots, S)$ ,  $l = \{1, 2, \dots, 20\}$ , which cover the fuzzy domain  $Y = [0, 1000]$ . These fuzzy subsets verify

$\forall y = P_l \in Y, \sum_{l=1}^{N_s} \mu_{B_l}(y) = 1$ , where  $P_l$  is the PVP generation and  $\mu_{B_l}$  is the membership function.

**According to relays control:** The relays command

requires  $N_s = 2$  fuzzy subsets.  $C_{jk} = (\text{grid}, \text{PVP})$  is the  $k^{\text{th}}$  fuzzy subset,  $k = \{1, 2\}$ , of the  $j^{\text{th}}$  apparatus relay. These fuzzy subsets cover the fuzzy domain  $Z = [0, 1]$  and verify

$$\forall z = ES_j \in Z, \sum_{k=1}^{N_s} \mu_{C_{jk}}(z) = 1, \text{ where } ES_j \text{ is the}$$

command given to the  $j^{\text{th}}$  apparatus relay and  $\mu_{C_{jk}}$  is the membership function.

The general rules format is:

IF ( $ER_1$  is  $A_{1i}$ ) and ( $ER_2$  is  $A_{2i}$ ) and

( $ER_3$  is  $A_{3i}$ ) and ( $ER_4$  is  $A_{4i}$ ) and

( $ER_5$  is  $A_{5i}$ ) and ( $ER_6$  is  $A_{6i}$ ) and ( $P_1$  is  $B_1$ )

THEN ( $ES_1$  is  $C_{1k}$ ) and ( $ES_2$  is  $C_{2k}$ ) and

( $ES_3$  is  $C_{3k}$ ) and ( $ES_4$  is  $C_{4k}$ ) and

( $ES_5$  is  $C_{5k}$ ) and ( $ES_6$  is  $C_{6k}$ )

**The fuzzification:** The determined fuzzy partitions lead to the determination of the following membership functions:

$$\mu_{A_{ji}}(x) = \max\left(0, 1 - \frac{|x_j - x_{0i}|}{\varepsilon_{x_{0i}}}\right) :$$

The membership function of the apparatus, (1)

$$\mu_{B_l}(y) = \max\left(0, 1 - \frac{|y - y_{0l}|}{\varepsilon_{y_{0l}}}\right) :$$

The membership function of PVP generation, (2)

$$\mu_{C_{jk}}(z) = \max\left(0, 1 - \frac{|z_j - z_{0k}|}{\varepsilon_{z_{0k}}}\right) :$$

The membership function of the relays states, (3)

where  $x_{0i}, y_{0l}, z_{0k}$  are respectively the real values of the variables  $x_j, y, z_j$  in their membership domains and  $\varepsilon_{x_{0i}}, \varepsilon_{y_{0l}}, \varepsilon_{z_{0k}}$  are respectively the range values of  $x_{0i}, y_{0l}, z_{0k}$ .

**Inference diagram:** By means of the rules' base already established and the membership functions obtained by the fuzzification operation, the weightings  $w_{jk}$  are computed according to Mamdani<sup>[17]</sup>.

**Acquire  $P_l$**

$l = E\left(\frac{P_l}{50}\right)$  : calculate the fuzzy subsets' number of the

PVP generation.

**Initialization:**  $ES_j = 0$  ( $j = 1$  to  $6$ ): all apparatus connected on the grid.

$ES_0 = 0, P_0 = 0 = 0$ : start pointers

**Repeat for  $j = 1$  to  $6$**

{Acquire  $j^{th}$  apparatus state  $ER_j$ }

**Fuzzification**

**Inference diagram**

$P_l = P_l - P_{j-1} * ES_{j-1}$ :  $P_l$  is the PVP generation,  $P_j$  is the operating power of the  $j^{th}$  apparatus.

$$w_{j1} = \min(\mu_{A_{j1}}, \mu_{B_{j1}})$$

$$w_{j2} = \min(\mu_{A_{j2}}, \mu_{B_{j+1}})$$

$$\mu_{C'_{j1}} = \min(w_{j1}, \mu_{c_{j1}})$$

$$\mu_{C'_{j2}} = \min(w_{j2}, \mu_{c_{j2}})$$

$$\mu_{C_j} = \max(\mu_{C'_{j1}}, \mu_{C'_{j2}})$$

**Defuzzification:** Compute  $ES_j$  (the  $j^{th}$  apparatus relay command) using the centroid method}.

**The system implementation:** The system is implemented at the Energy and Thermal Research Centre (CRTE) in the north of Tunisia since January 2005. It includes:

- \* 1 kWp PVP and the electric grid as energy sources. The PVP is equipped with a Maximum Power point Tracker (MPPT)<sup>[13]</sup> which is an electronic device that monitors PVP generation to operate near its maximum power point along the I-V curve and an inverter that provides the same output voltage as the electric grid (230V/50Hz)<sup>[7]</sup>.
- \* Six household apparatus of different power: 50, 100, 200, 300, 400 and 500W (230V/50Hz). Each one is controlled by a two position relay in order to be connected either to the PVP output or to the electric grid.

Figure 2 shows the connection schema of the system components. The decision centre is composed of a personnel computer equipped with a data acquisition and control card. The PVP generation ( $P_l$ ) is calculated on the basis of a published 1kWp PVP validated model<sup>[15]</sup>:

$$P_l = 20 \begin{pmatrix} 3.33 + 1.210^{-3} \left( \frac{I}{1000} \right) \left( T_a + \frac{I}{40} - 25 \right) \\ + 3.35 \left( \frac{I}{1000} - 1 \right) \end{pmatrix} u_{pv} \quad (4)$$

where  $I$  and  $T_a$  are respectively the acquired solar radiation ambient temperature measured at the surface of the PVP.  $u_{pv}$  is the PVP output voltage fixed to 12V by the MMPT device. The algorithm is implemented using the Matlab software as a programming tool.

After implementation, the system has been tested during the year 2005. All its input/output ( $T_a, I, ER_j, ES_j$ ) have been daily recorded using a time step of 5 minutes. A power audit has been also

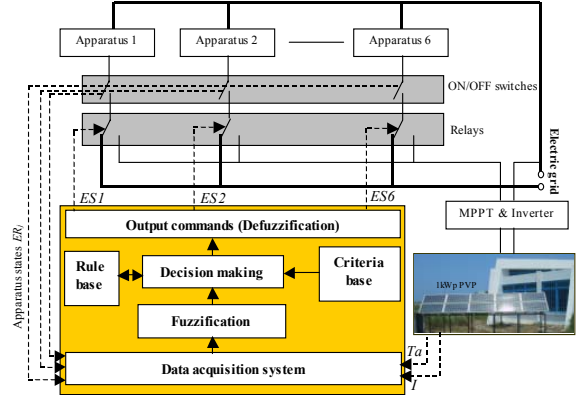


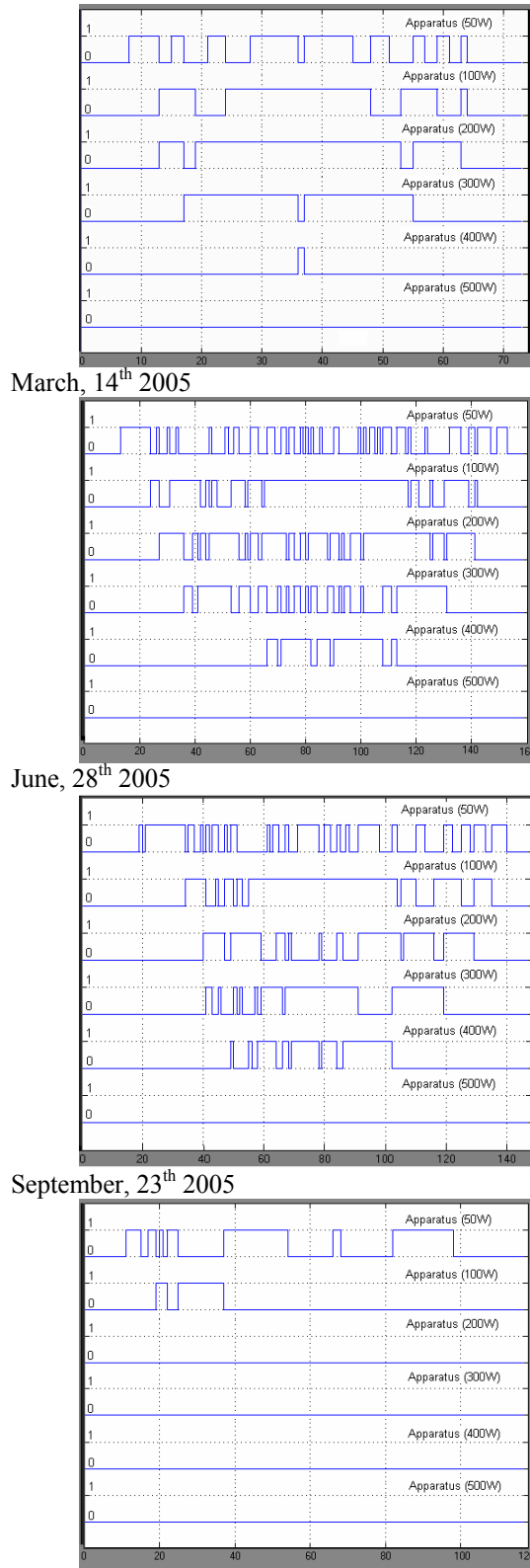
Fig. 2: System components and implementation

established in order to determine the system performance. Even so, for clearness reason the system behaviour and performance is given only for four days representing the year's seasons. Figure 3 shows the fuzzy commands timing of relays during daylight. During function, all apparatus were switched on in order to evaluate the contribution of the PVP generation to the whole installation. By examining the fuzzy decisions, it can be easily deduced that most commutations between grid and PVP output are observed at apparatus of lower power. This is due to the above management constraints (§2) which affect the higher priority to apparatus of lower power in order to recuperate the remaining power of the ones of higher power. As well, commutations can be seen at apparatus of high power when PVP generation is available (June and September). In this case these commutations are limited to the time around midday. Finally, only lower power apparatus are connected to PVP output while PVP generation is weak (December).

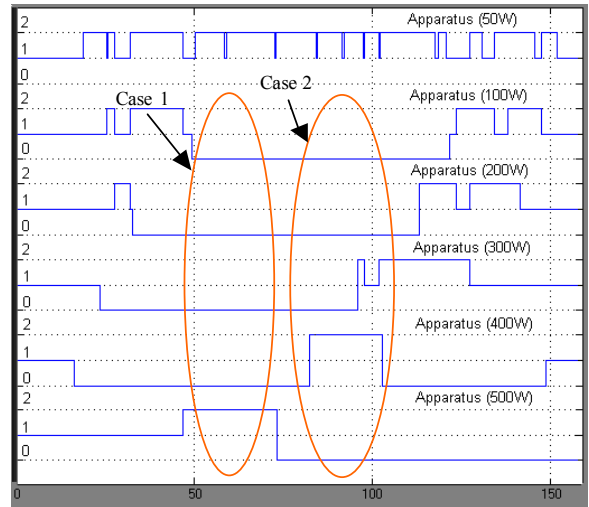
Since it holds the lower priority, the apparatus of 500 W could not be connected to the PVP output unless other apparatus are switched off and there is enough PVP generation (Fig. 4). In fact, in case 1 all apparatus of 100W to 400W are switched off to give the chance to apparatus of 500W to be connected to PVP output. However, in case 2, the apparatus of 500W is switched off and as a consequence any other apparatus will be connected to PVP output, respecting management criteria (§2), as soon as it is switched on.

**Approach valorisation:** The valorisation of the designed system consists of daily and monthly assessments.

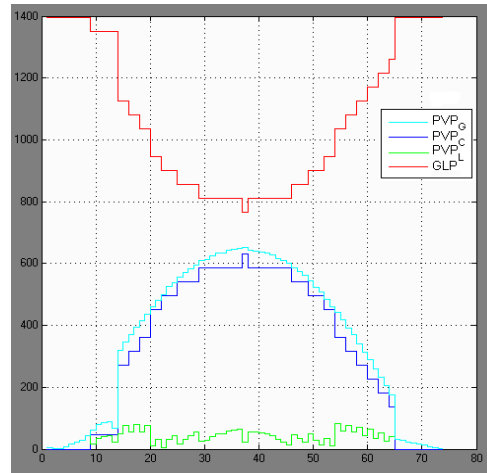
**Daily assessment:** The approach assessment is ensured by the establishment of a daily power audit. Figure 5 plots in real time the curves of the PVP related powers (PVP<sub>G</sub>: generated, consumed: PVP<sub>C</sub>, lost: PVP<sub>L</sub>) and of the power load from grid (GLP) during the four chosen representative days (§4). It is noted that the curve of PVP<sub>C</sub> follows the variations of PVP<sub>G</sub> in order to minimise PVP<sub>L</sub>. Similarly, GLP decreases considerably



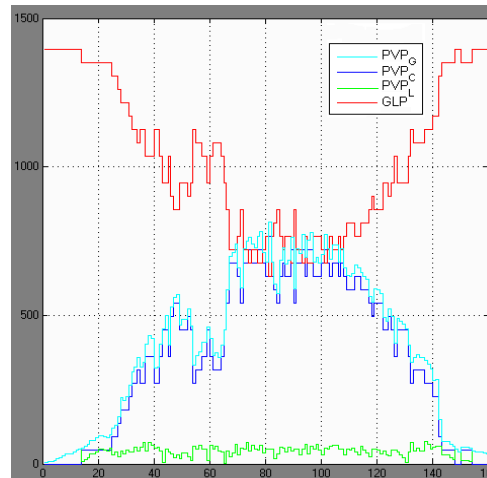
December, 10<sup>th</sup> 2005  
 Fig. 3: Timing of commands given to apparatus relays (all apparatus switched on). X\_axis: 1 unit = 5mn of the daylight. Y\_axis: 0: apparatus connected to PVP output. 1: apparatus connected to grid



August, 8<sup>th</sup> 2005  
 Fig. 4: Timing of relays commands (apparatus manipulated). X\_axis: Time: 1 unit = 5mn of the daylight. Y\_axis: Apparatus state: 0: switched off. 1: connected to grid. 2: connected to PVP output



March, 14<sup>th</sup> 2005



June, 28<sup>th</sup> 2005

Table 1: The monthly effectiveness coefficient

	Jan.	Feb.	Mar.	Apr.	May	Jun.	Jul.	Aug.	Sep.	Oct.	Nov.	Dec.
PVP <sub>GE</sub>	86,2	98,8	129,1	135,2	148,3	149,4	156,4	161,3	136,9	123,3	92,5	78,6
PVP <sub>CE</sub>	69,8	85,7	115,8	120,2	129,8	133,7	139,2	145,4	122,2	109,5	79,3	62,8
PVP <sub>LE</sub>	16,4	13,1	13,3	15	18,5	15,7	17,2	15,9	14,7	13,8	13,2	15,9
η%	81,0	86,7	89,7	88,9	87,5	89,5	89	90,1	89,3	88,8	85,7	79,9

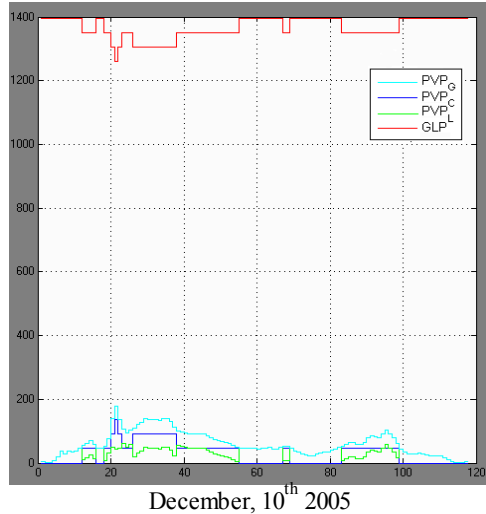
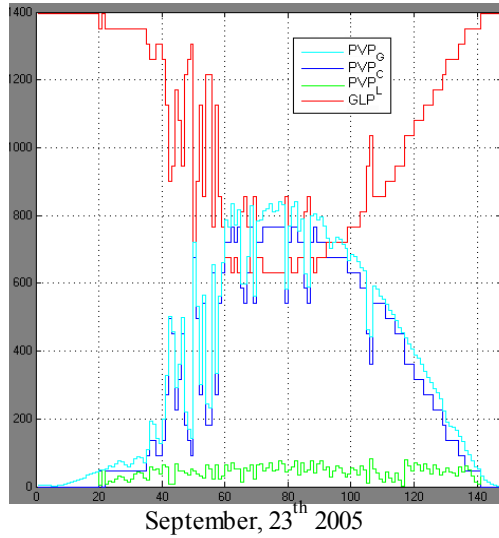


Fig. 5: The daily power audit. X\_axis: 1 unit = 5mn of the daylight/ Y\_axis: the power (W)

around midday especially during days of sunny seasons. These interpretations confirm the approach contribution in term of energy save and management for the whole installation.

**Monthly assessment:** The same study was renewed to form a monthly energy balance (Fig. 6) so as to prove the effectiveness of the management approach. All PVP related powers are integrated over daylight (from sunrise (SR) to sunset (SS)). Obtained energies are cumulated over the month length (ML) to compute PVP monthly energies (generated: PVP<sub>GE</sub>, consumed: PVP<sub>CE</sub>, lost: PVP<sub>LE</sub>) as follows:

$$PVP_{GE} = \sum_{j=1}^{ML} \int_{SR(j)}^{SS(j)} PVP_G(t) dt ;$$

$$PVP_{CE} = \sum_{j=1}^{ML} \int_{SR(j)}^{SS(j)} PVP_C(t) dt ;$$

$$PVP_{LE} = \sum_{j=1}^{ML} \int_{SR(j)}^{SS(j)} PVP_L(t) dt$$

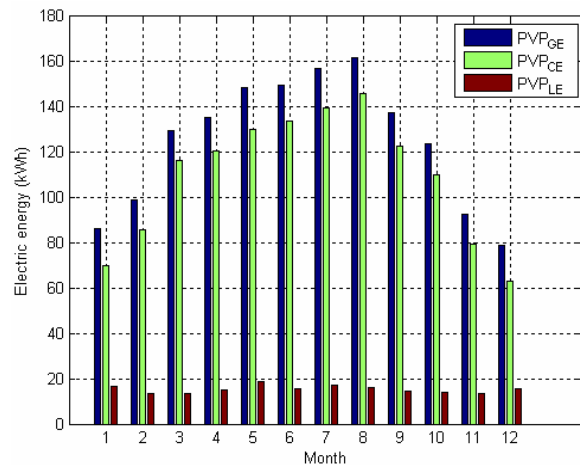


Fig. 6: The monthly energy balance

While the electric energy produced by the PVP varies between 80 and 160 kWh/month, the electric energy consumed from the PVP varies between 65 and 145 kWh/month which involves an unused energy about 15 kWh/month. This lost energy is generally produced during the sunrise and sunset times where PVP generation is insufficient (<50W) to supply energy for even the lower power apparatus. A second valorisation consists of the calculation of a monthly effectiveness coefficient defined by:

$$\eta\% = \frac{PVP_{GE} - PVP_{LE}}{PVP_{GE}} \times 100 = \frac{PVP_{CE}}{PVP_{GE}} \times 100$$

Table 1 gives the (η%). This coefficient is almost constant through the months of the year and it varies between 80% and 90% which justifies the continuous energy save contribution of the proposed solution.

## CONCLUSION

The efficient management of the energy produced by a conversion system depends on consumption needs

on the one hand and on the supplied energy (generated by the conversion system) on the other hand. Herein the energy produced by a PVP of 1000Wp is optimally managed to provide a complementary energy for household apparatus so as to offer a maximum energy saving. The management approach consists of deciding the optimal connection mode of domestic apparatus either to PVP output or to grid. Decision is made on the basis of PVP generation and apparatus states according to criteria which offer a maximum exploitation of the energy delivered by the PVP during daylight. The system is implemented and tested during 2005. A carried out energetic audit confirms that 90% of PVP generated energy is brought to the installation as energy save.

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